Compactness of the complex Green operator

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We indicate a new proof for, and a slight improvent of, a recent result of A. Raich on compactness of the complex Green operator on a CR-submanifold of \mathbb{C}^n of hypersurface type. Let M be a smooth compact pseudoconvex CR-submanifold of \mathbb{C}^n of hypersurface type, let $\dim_{\mathbb{C}} T_z^{1,0}(M) = m - 1, z \in M$, and let $1 \leq q \leq m - 2$. If M satisfies property(P_q) and property(P_{m-1-q}), then the complex Green operator on (0,q)-forms is compact. Our proof is based on the fact that locally, M is CR-equivalent to an actual hypersurface, and the corresponding compactness result of Raich and the author for boundaries of domains.