## Hints for solving the exercises in Chapter 2

Hints to Exercise 2.1 The local representation

$$s(x) = a_k + b_k(x - x_k) + c_k(x - x_k)^2$$
 for  $x \in [x_k, x_{k+1}], \quad k = 0, 1, \dots, N-1,$ 

and the differentiability conditions as well as the interpolation conditions lead to a linear system of N equations for the N + 1 coefficients  $b_0, b_1, \ldots, b_{N-1}, b_N$  with the auxiliary variable  $b_N = 2h_{N-1}c_{N-1} + b_{N-1}$ . The additionally given condition in part (a) of this exercise results in a linear system of N + 1 equations for the N + 1 unknown coefficients  $b_0, b_1, \ldots, b_N$ , and the additionally given condition in part (b) of the exercise results in a linear system of N equations for the N unknown coefficients  $b_1, b_2, \ldots, b_N$ . Consider then the system matrices corresponding to the given linear systems of equations, respectively. In part (b), determine the determinant of this matrix by an expansion along the first row.

**Hints to Exercise 2.3** Use the same procedure as in the estimate of the error for cubic spline interpolation (w.r.t. to the third derivative).