# Moment Problems for Real Measures on the Unit Circle 

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In this talk we are considering the following problem: when are the given complex numbers $\left(c_{j}\right)_{j=-n}^{n}, c_{-j}=\overline{c_{j}}$, the first moments of a real Borel measure $\mu=\mu^{+}-\mu^{-}$on $\mathbb{T}$, such that $\mu^{-}$is supported on a set of at most $k$ points. A necessary and sufficient condition is that the Toeplitz matrix $T=\left(c_{i-j}\right)_{i, j=0}^{n}$ is a certain real linear combination of rank 1 Toeplitz matrices. For $k>0$, this is more general than the condition that $T$ admits self-adjoint Toeplitz extensions with $k$ negative squares. For a singular $T$, an equivalent condition is that a certain polynomial has all its roots on $\mathbb{T}$. We also discuss the situation when $T$ is invertible.

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