

# Numerical Analysis II

## Homework Sheet 12

### Exercises

#### Tutorial on July 14

#### 1. Problem

Apply the procedure (P) in order to determine the differentiation-index of the DAE

$$\begin{bmatrix} 0 & 0 \\ 1 & -t \end{bmatrix} \dot{x}(t) = \begin{bmatrix} -1 & t \\ 0 & 0 \end{bmatrix} x(t) + \begin{bmatrix} f_1(t) \\ f_2(t) \end{bmatrix}.$$

#### 2. Problem

Using procedure (P), determine the maximal constraint level of the DAE arising from physical multi-body systems

$$\begin{aligned} \dot{p}(t) &= v(t), \\ M(p(t))\dot{v}(t) &= f(p(t), v(t), t) - G(p(t), t)^T \lambda, \\ 0 &= g(p(t), t), \end{aligned}$$

where  $M(p)$  is positive definite and  $G(p(t), t) = \frac{\partial}{\partial p} g(p, t)$  has full row rank.

**No Theoretical Homework**