Self-adjoint extensions with several gaps: scalar-type Weyl functions

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Let S be the orthogonal sum of infinitely many pairwise unitarily equivalent symmetric operators with non-zero deficiency indices. Further, let J be the union of disjoint gaps of S. If there is a self-adjoint extension S_0 of S such that J is contained in the resolvent set of S_0 and the associated Weyl function of the pair $\{S, S_0\}$ is monotone with respect to J, then for any self-adjoint operator R there is a self-adjoint extension $\widetilde{S}$ such that the spectral parts $\widetilde{S}_J$ and R_J are unitarily equivalent.