Classes of operators in a Krein space: relations

L.I. Sukhocheva

This talk is based on a joint work with T. Azizov and V. Strauss.

Let $\mathcal{K} = \mathcal{K}^+ \oplus \mathcal{K}^-$ be a Krein space, let

$$A = \begin{bmatrix} A_{11} & A_{12} \\ & & \\ A_{21} & A_{22} \end{bmatrix}$$

be a bounded selfadjoint operator in \mathcal{K} .

(i) We denote by $\mathfrak{S}_{\infty,12}$ the operators A with a compact component A_{12} .

(ii) the operator A is called definitizable if there exists a polynomial p such that p(A) is a nonnegative operator.

(iii) the operator A belongs by definition to the class (**H**) if it has a maximal nonnegative invariant subspace and each of such subspaces is a direct sum of the finite dimensional isotropic part and a uniformly positive subspace. We say that $A \in \mathbf{K}(\mathbf{H})$ if A commutes with an operator of the class (**H**).

(iv) if A has a maximal nonnegative invariant subspace as in (iii) we say that $A \in D_{\kappa}^{+}$.

The aim of this talk is to show relations between operator classes (i)–(iv).

The research is supported by the grant RFBR 02-01-00353.