M-functions for closed extensions of adjoint pairs of operators

I. Wood joint work with M.B. Brown, G. Grubb, J. Hinchcliffe, M. Marletta and S. Naboko

We consider the generalisation of the Weyl m-function from Sturm-Liouville problems and the Dirichlet-to-Neumann map from PDEs to the setting of adjoint pairs of operators. We show that in this setting every closed extension of a minimal operator is associated with an abstract M-function and discuss spectral properties of the extension via the M-function. The results can be applied to elliptic PDEs.