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# **Exploring the Weather-Climate Connection: Probabilistic Climate Dynamics Part I : An Introduction to the Climate System**

Adam Monahan

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School of Earth and Ocean Sciences, University of Victoria



# Overview

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  - Climate change
  - Multiple scales of variability
  - Weather, climate, and probability



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# Earth, Ocean, Atmosphere: Scale

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- Earth is (roughly) spherical



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⇒ large-scale motions quasi-2D

- “Vertical” motion tends to be episodic, localised, turbulent

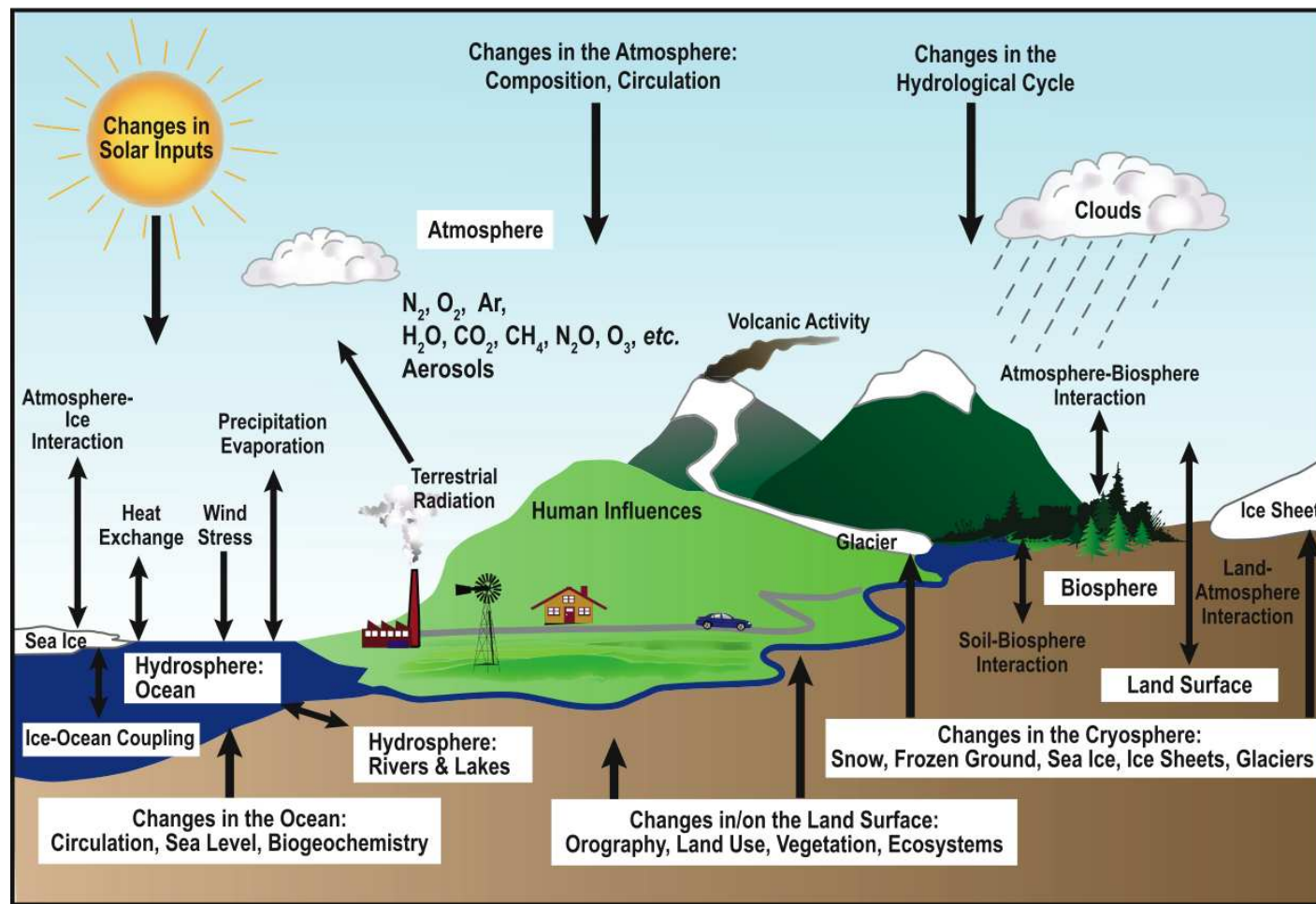
# Earth, Ocean, Atmosphere: Scale

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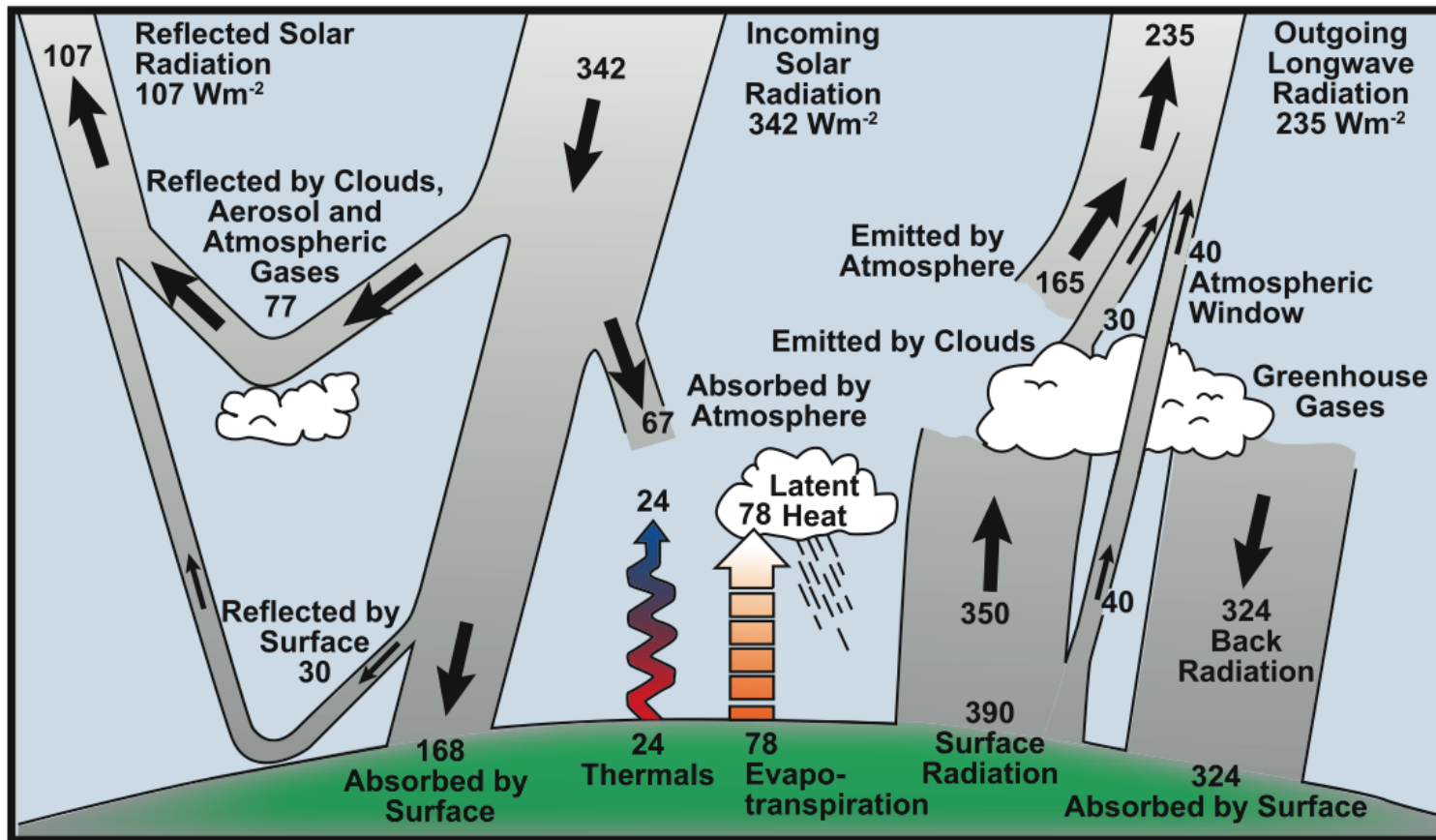
# Earth, Ocean, Atmosphere: The Climate System



From IPCC AR4 <http://www.ipcc.ch>

FAQ 1.2, Figure 1

# Earth's Radiation Balance

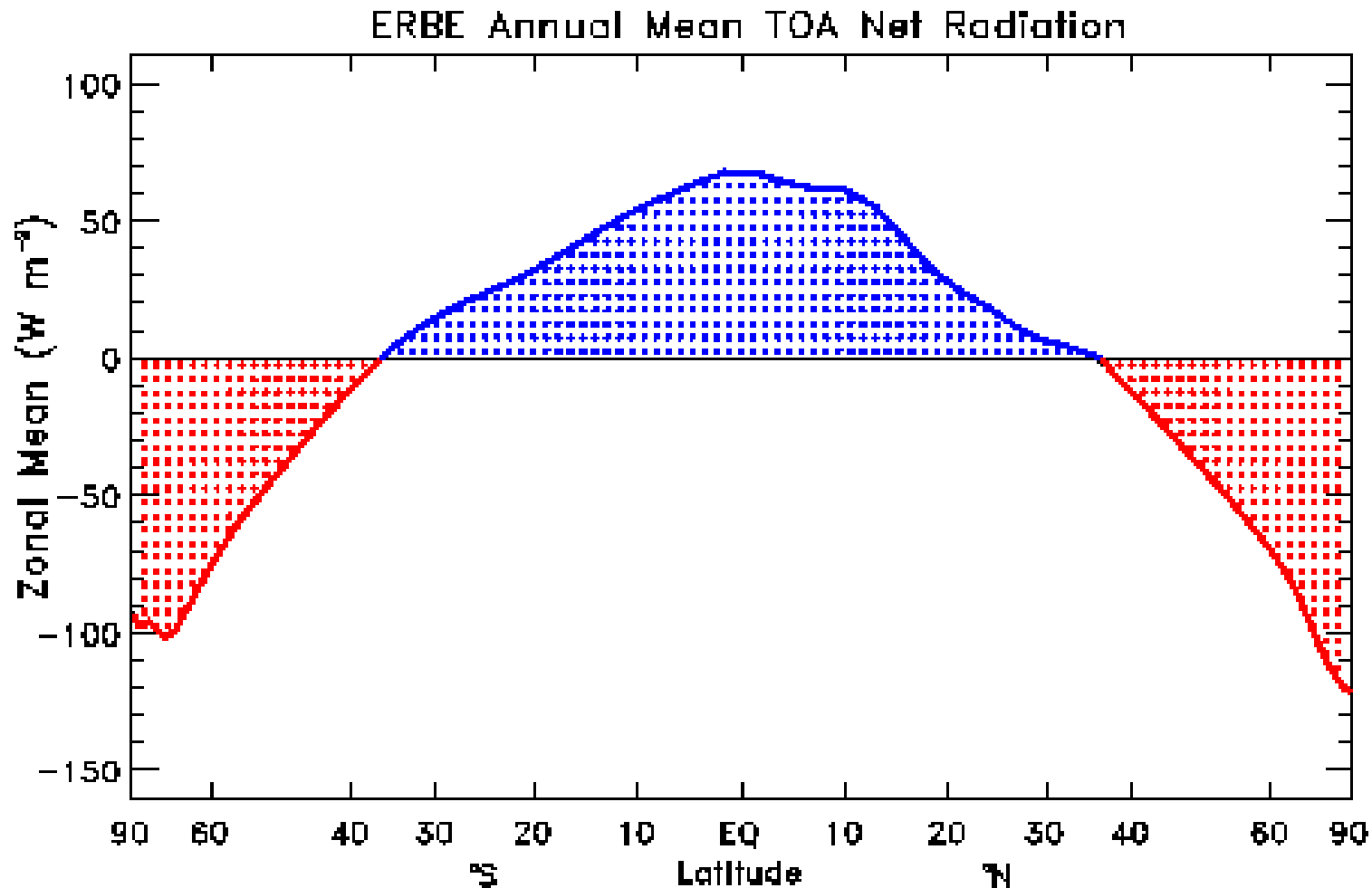


From IPCC AR4 <http://www.ipcc.ch>



# Earth As A Heat Engine

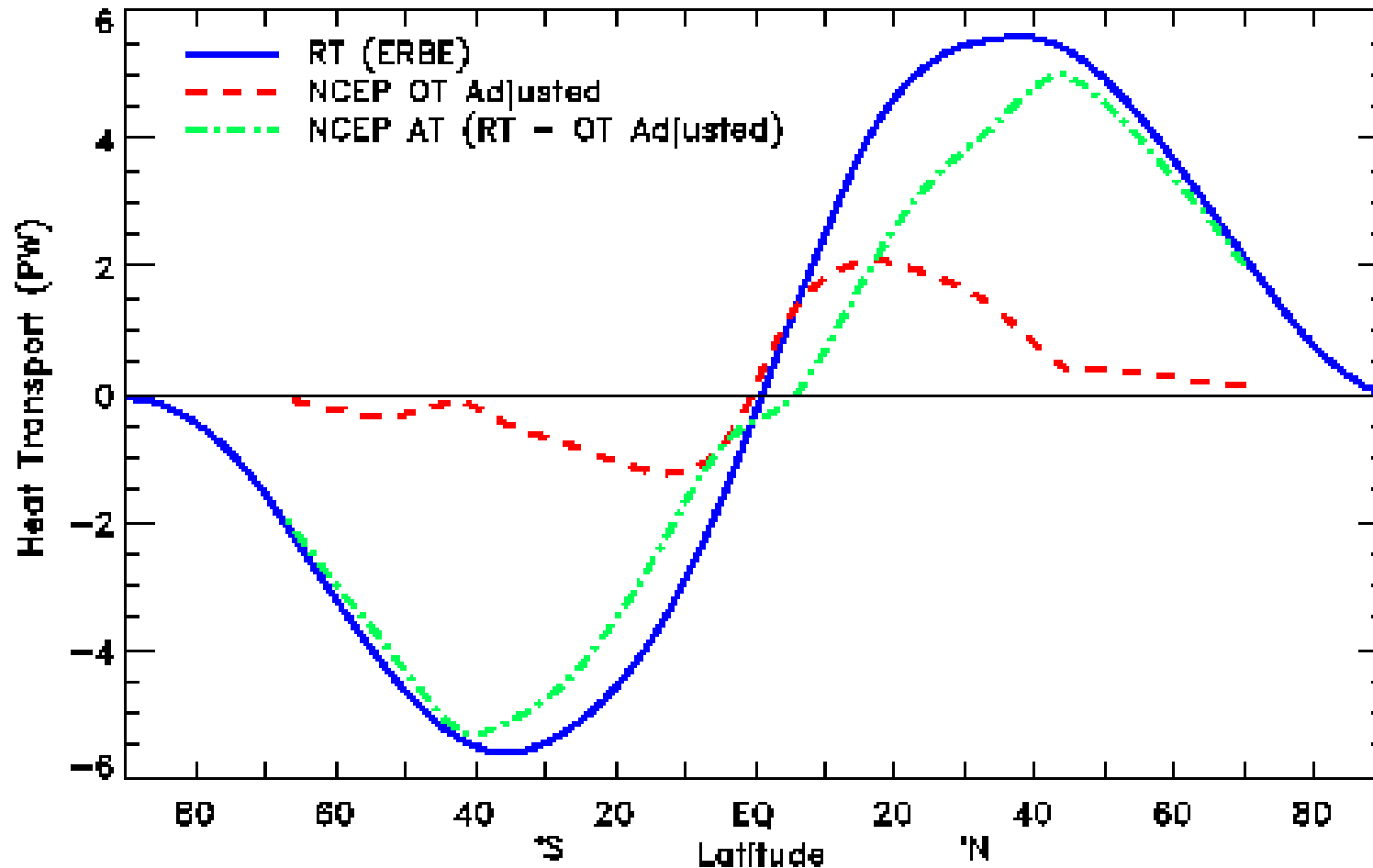
Solar energy in - terrestrial energy out



From Trenberth and Caron, J. Clim, 2001

# Earth As A Heat Engine

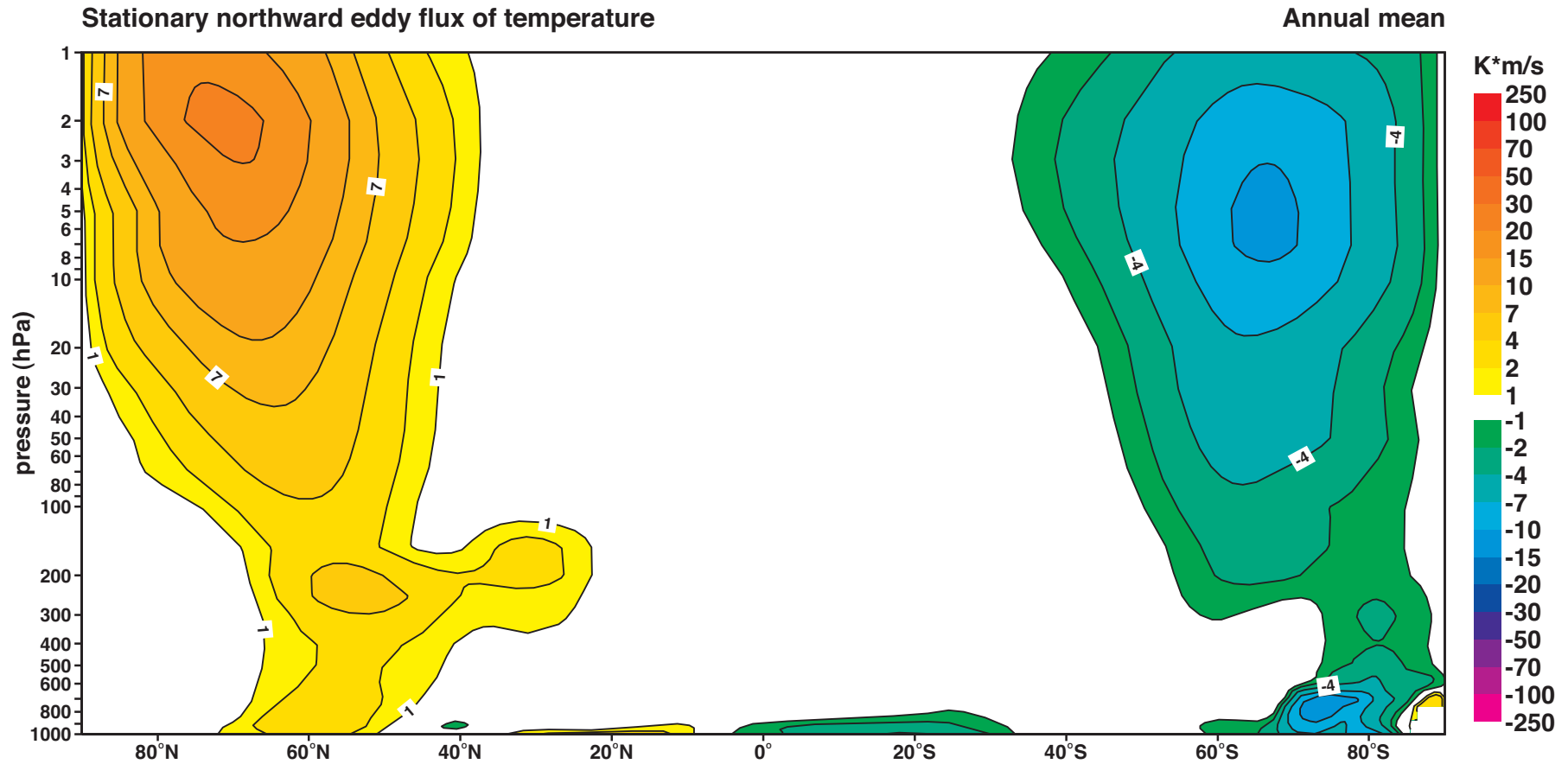
Meridional (northwards) equilibrium heat transport



From Trenberth and Caron, J. Clim, 2001

# Earth As A Heat Engine

## Mean northwards heat flux by mean state



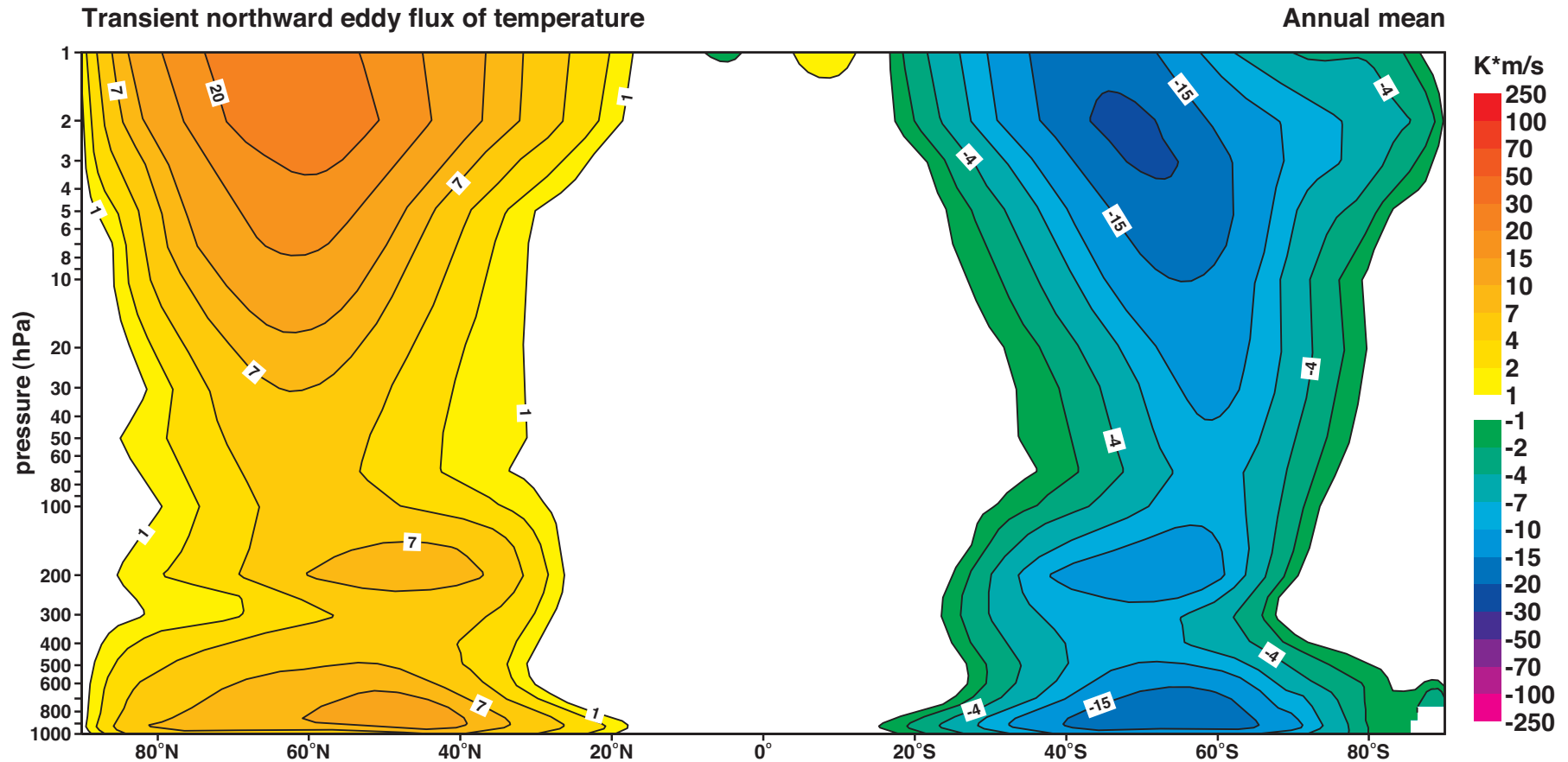
From ERA 40 Reanalysis Atlas



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# Earth As A Heat Engine

## Mean northwards heat flux by transient variability

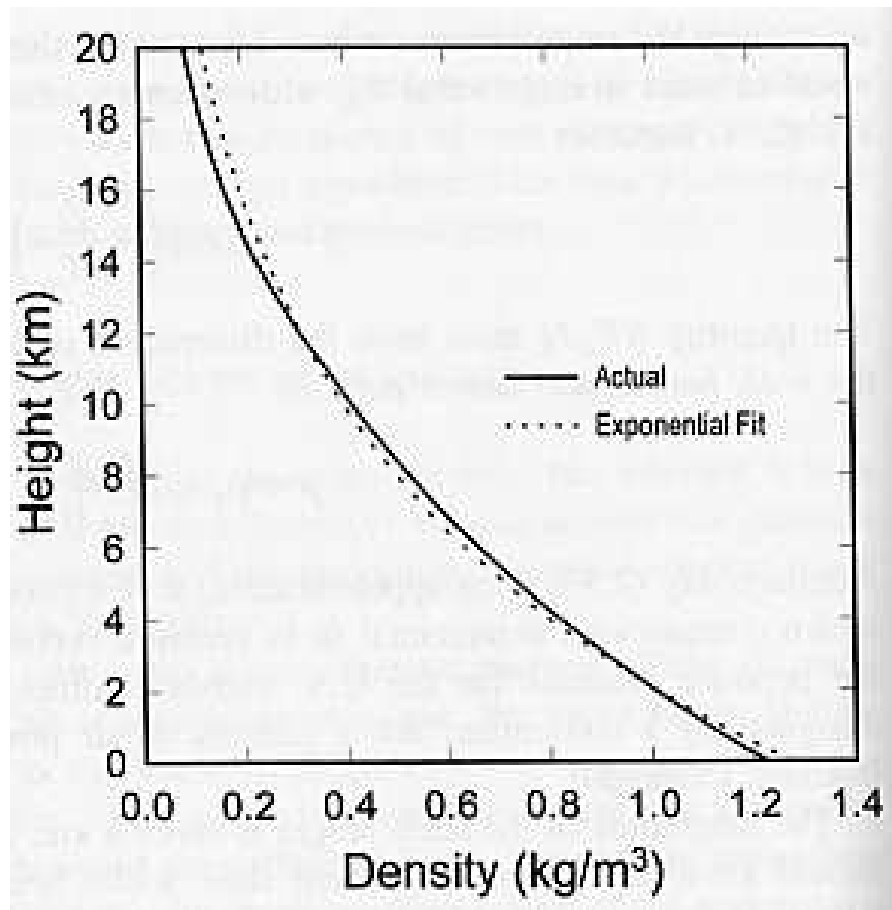


From ERA 40 Reanalysis Atlas

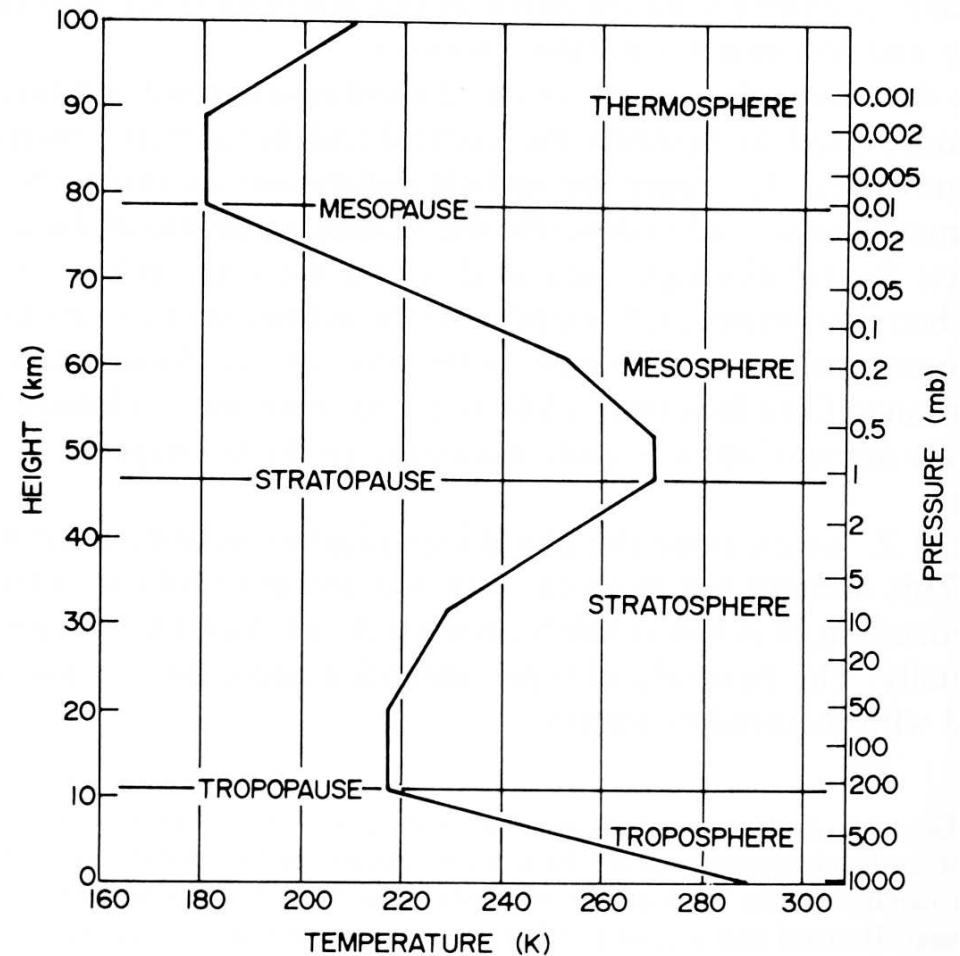


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# Atmosphere: Mean Vertical Structure



From Bohren & Albrecht 1998



From Wallace & Hobbs 1977

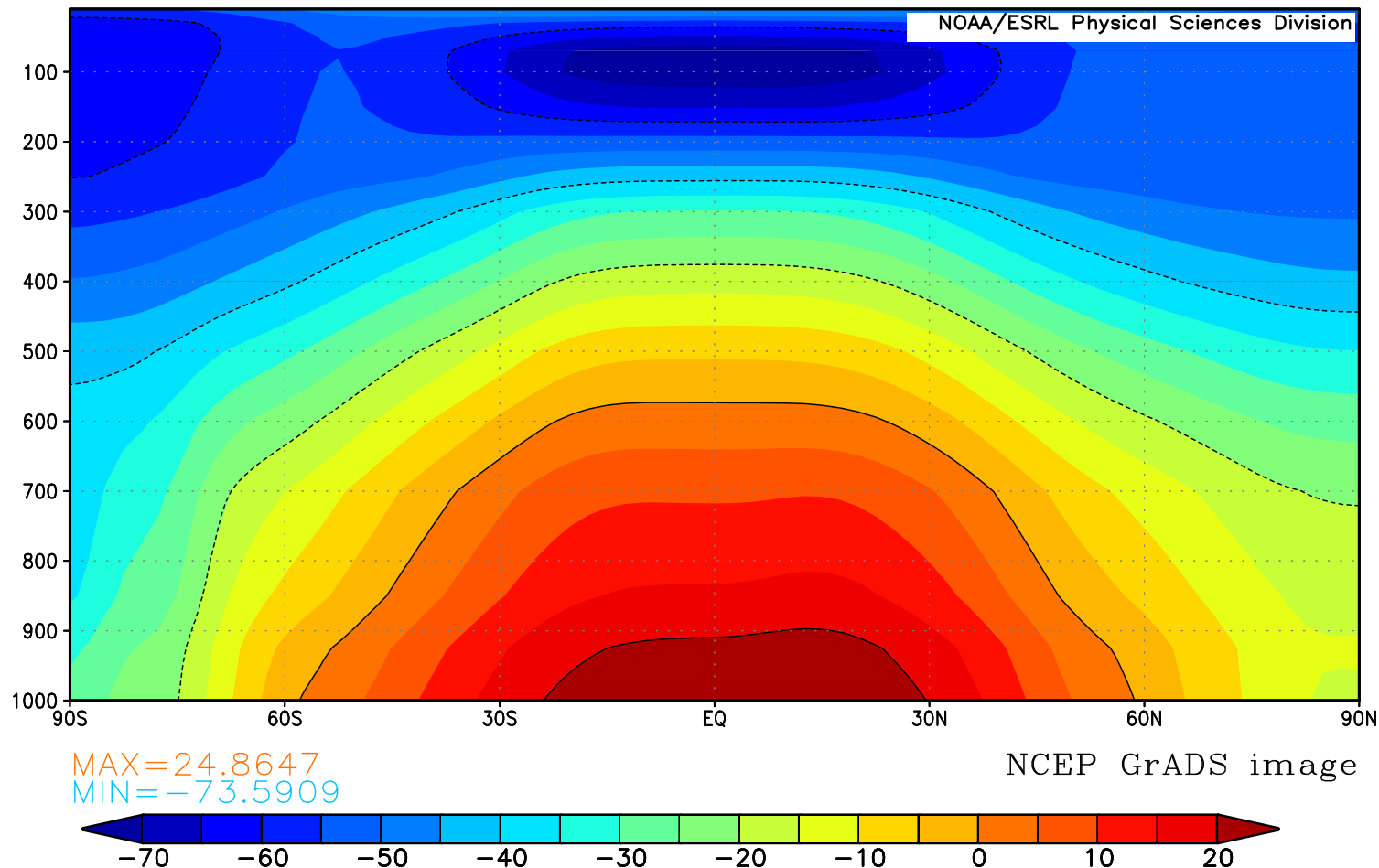


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# Atmosphere: Mean Air Temperature

lat: plotted from -90 to 90.00  
lev: plotted from 1000.0000 to 10.0000  
lon: averaged over 0.0000 to 357.5000  
t: averaged over Jan to Dec

Monthly Longterm Mean (1968–1996) air degC

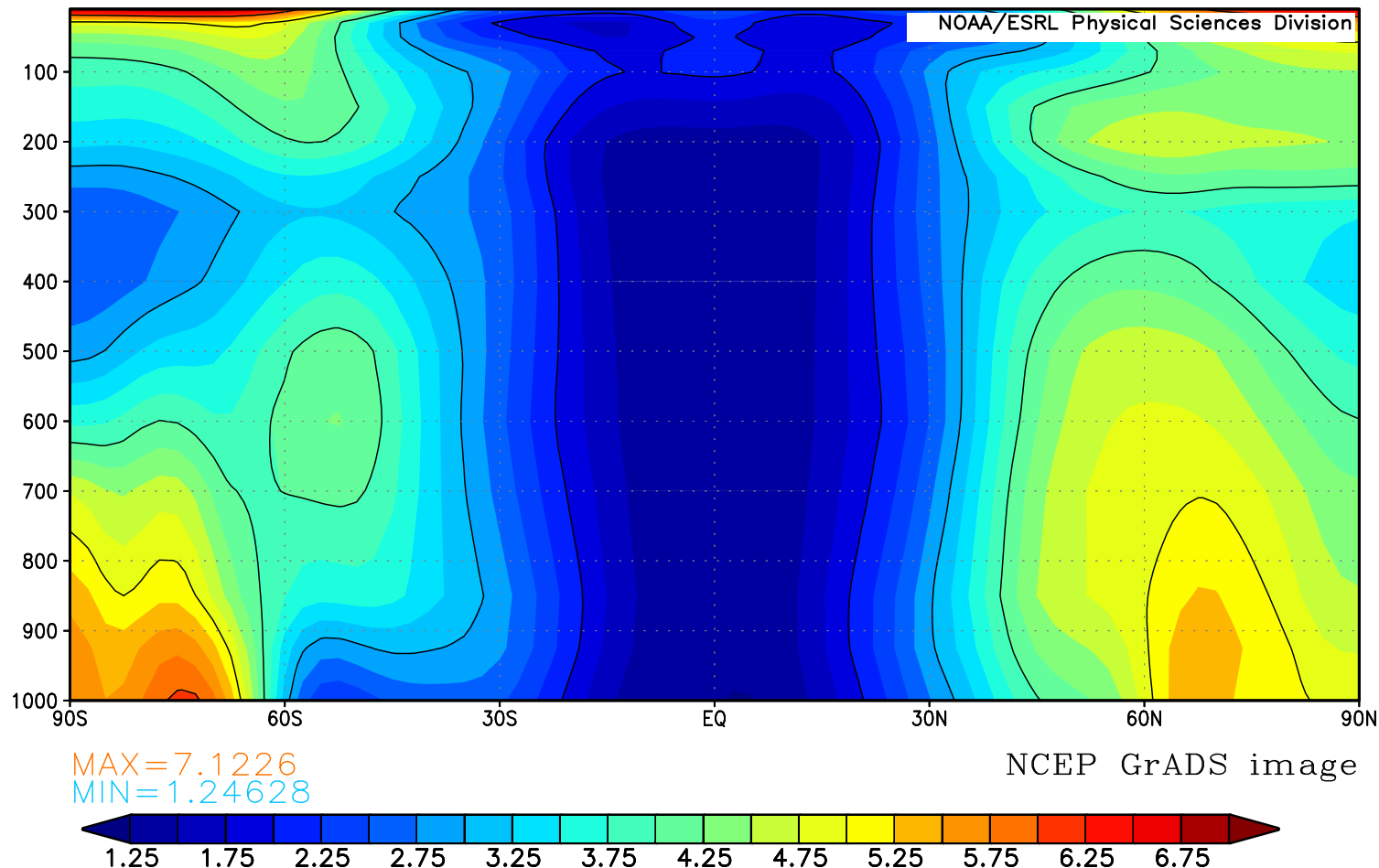


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# Atmosphere: Standard Deviation of Air Temperature

lat: plotted from -90 to 90.00  
lev: plotted from 1000.0000 to 10.0000  
lon: averaged over 0.0000 to 357.5000  
t: averaged over Jan to Dec

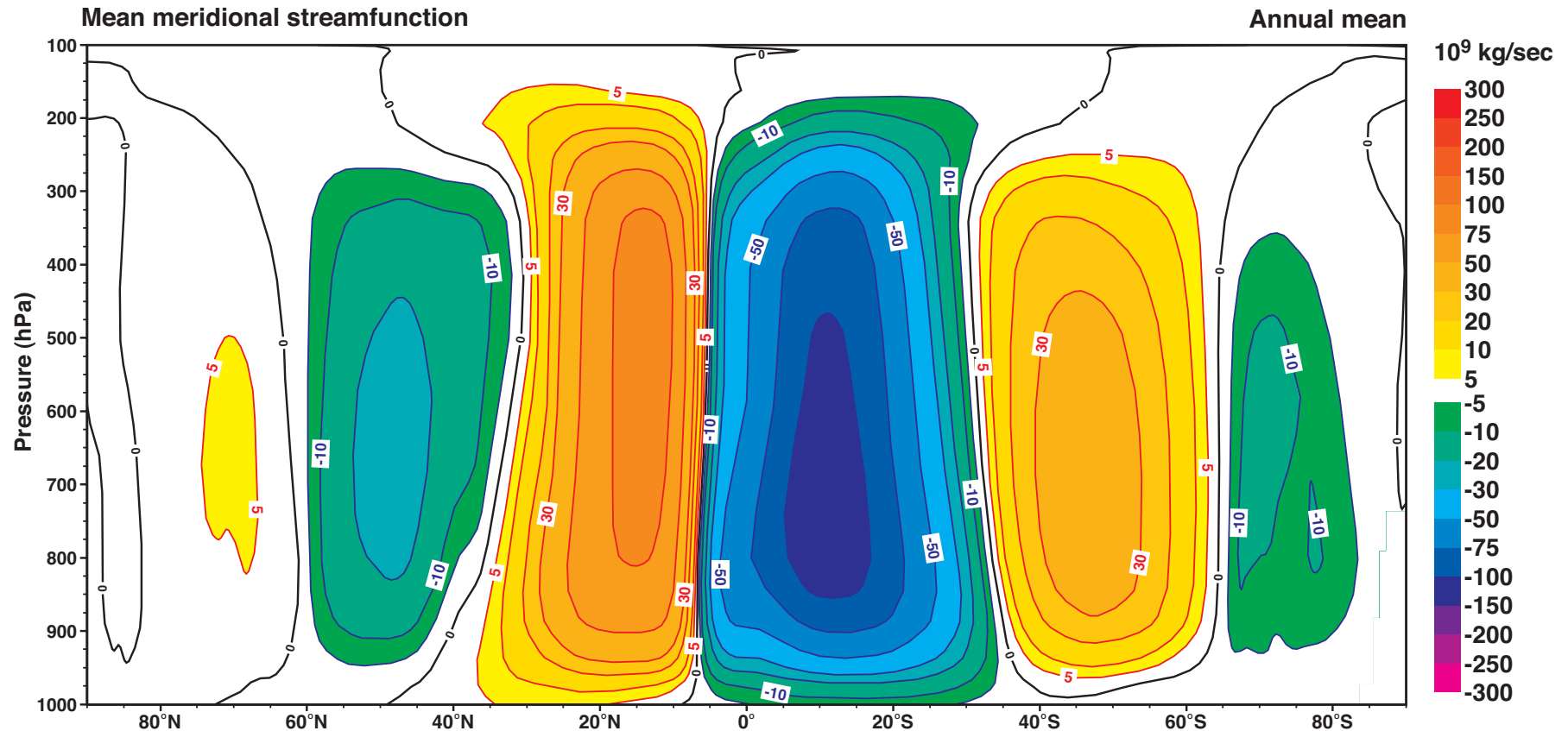
Total Standard Deviation (by Month) air degC



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# Atmosphere: Mean Meridional Circulation

## Zonal mean meridional circulation



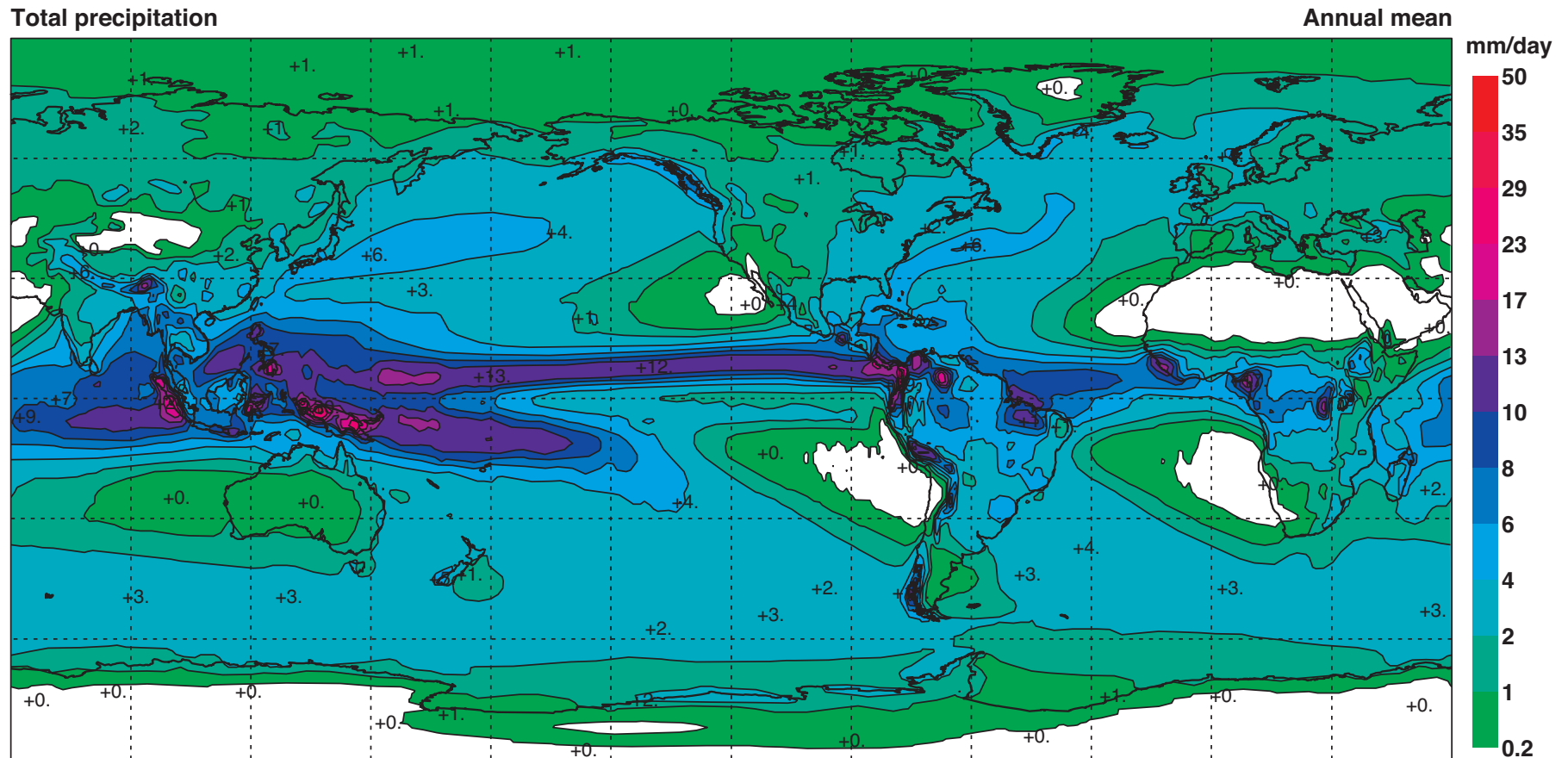
From ERA 40 Reanalysis Atlas



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# Atmosphere: Mean Precipitation

## Annual mean precipitation



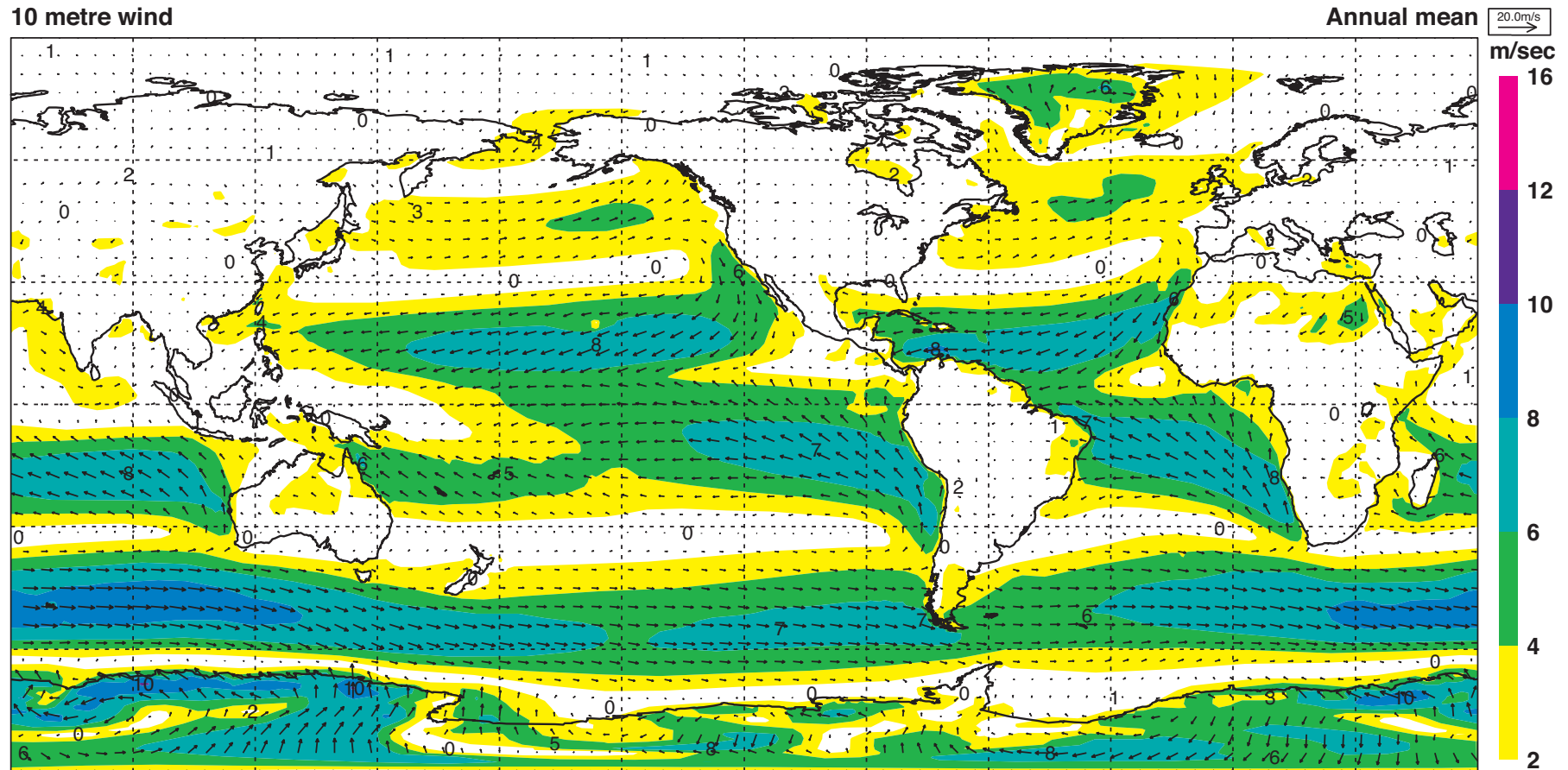
From ERA 40 Reanalysis Atlas



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# Atmosphere: Mean Surface Winds

## Mean 10 m surface winds



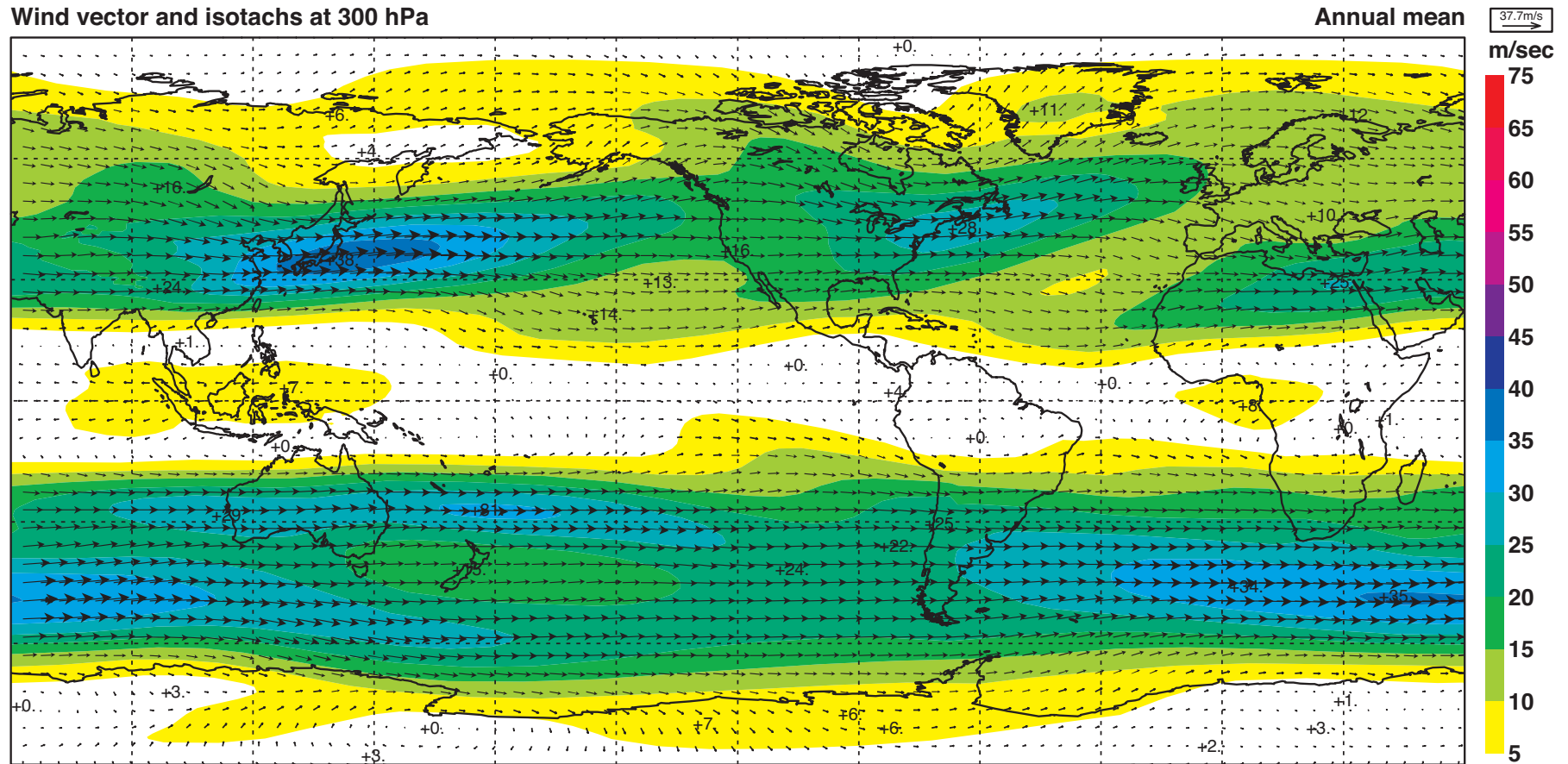
From ERA 40 Reanalysis Atlas



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# Atmosphere: Mean Upper Tropospheric Winds

## Mean 300 hPa winds



From ERA 40 Reanalysis Atlas

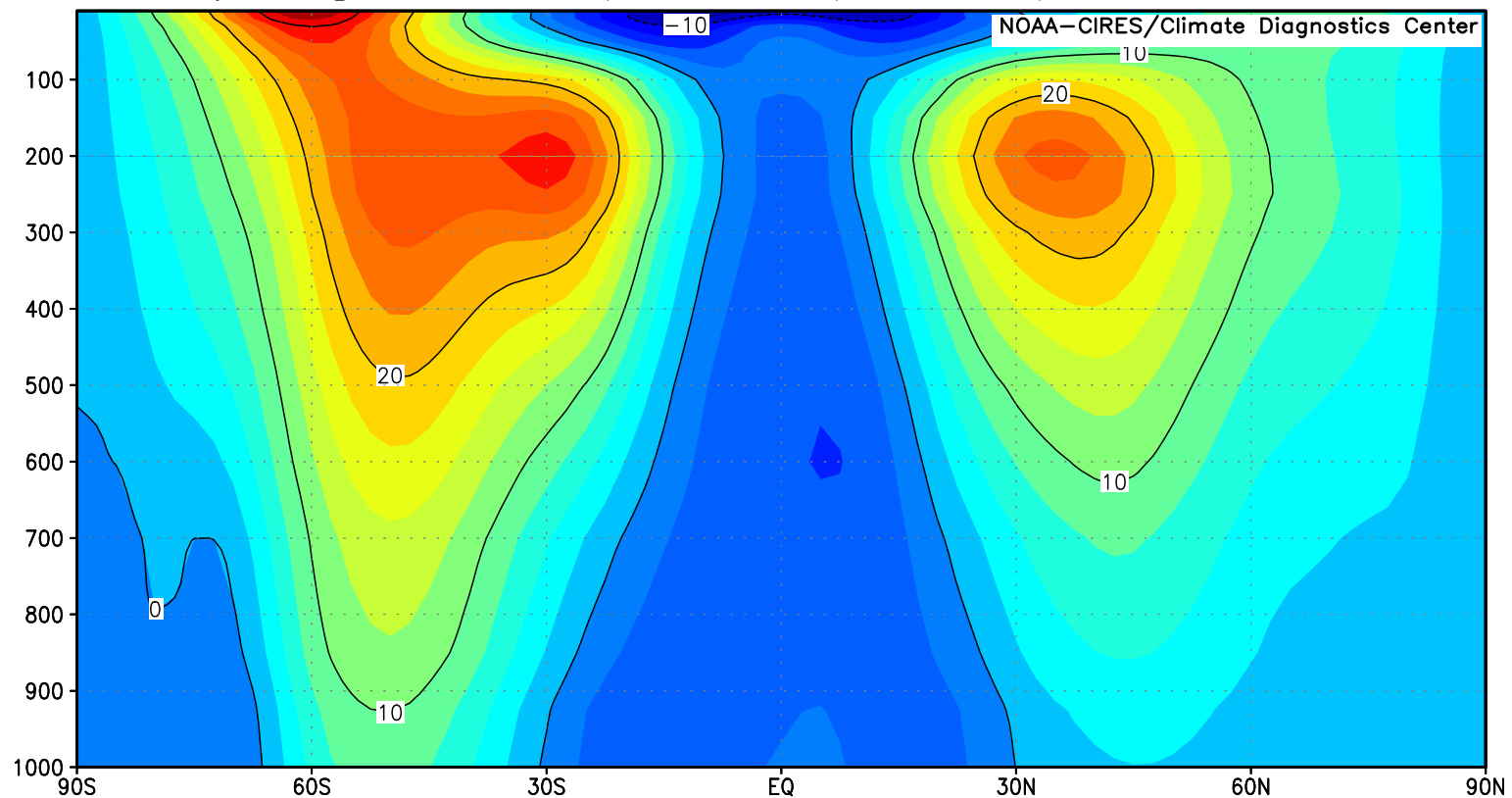


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# Atmosphere: Mean Zonal Wind

lat: plotted from -90 to 90.00  
lev: plotted from 1000.0000 to 10.0000  
lon: averaged over 0.0000 to 357.5000  
t: averaged over Jan to Dec

Monthly Longterm Mean (1968–1996) uwnd m/s

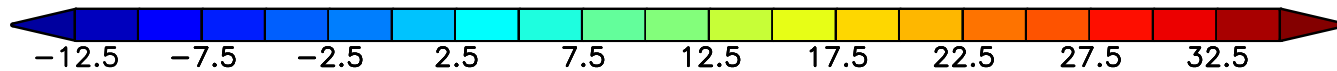


MAX = 35.1597  
MIN = -14.7143

NCEP GrADS image



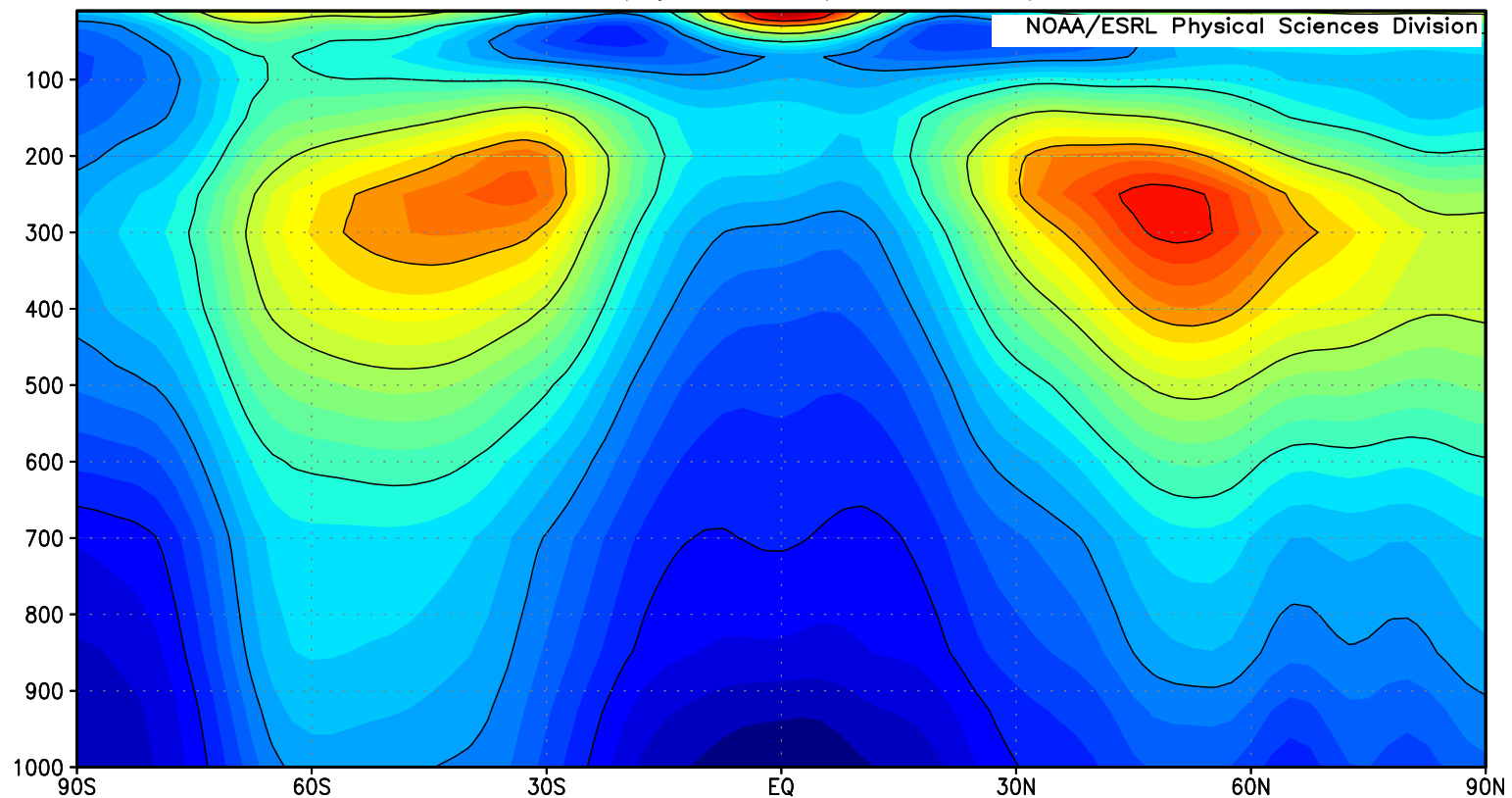
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# Atmosphere: Standard Deviation of Zonal Wind

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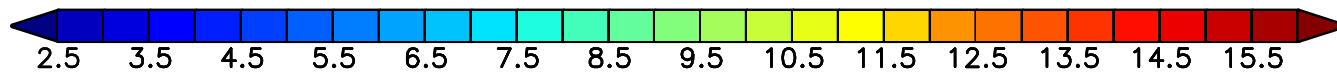


MAX=16.0314  
MIN=2.0851

NCEP GrADS image



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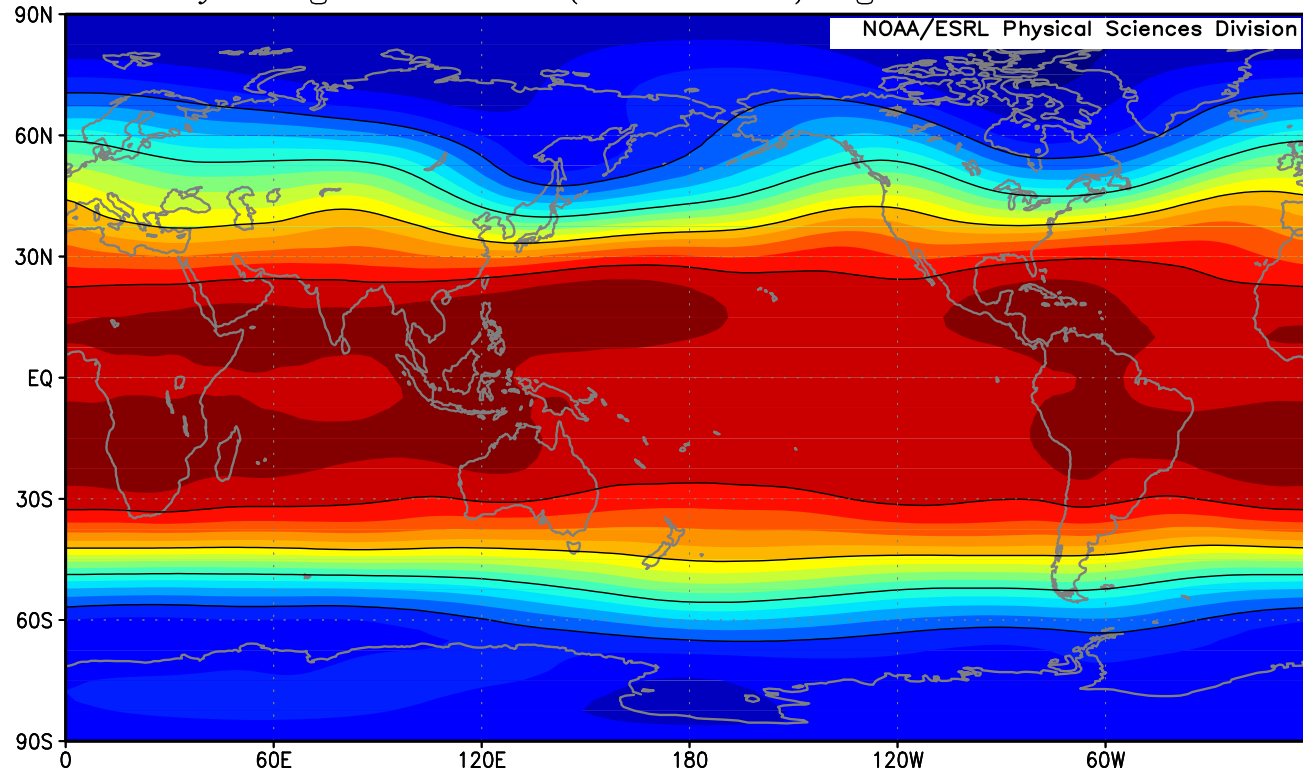


# Atmosphere: Mid-Troposphere Streamlines

## Time-mean December geopotential height

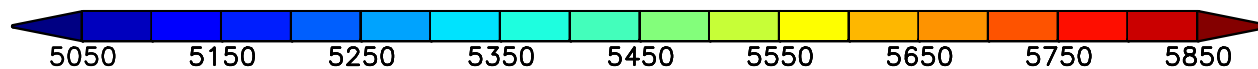
lat: plotted from -90 to 90.00  
lon: plotted from 0.00 to 357.50  
lev: 500.0000  
t: Dec

Monthly Longterm Mean (1968–1996) hgt m



MAX=5877.4  
MIN=5037.2

NCEP GrADS image

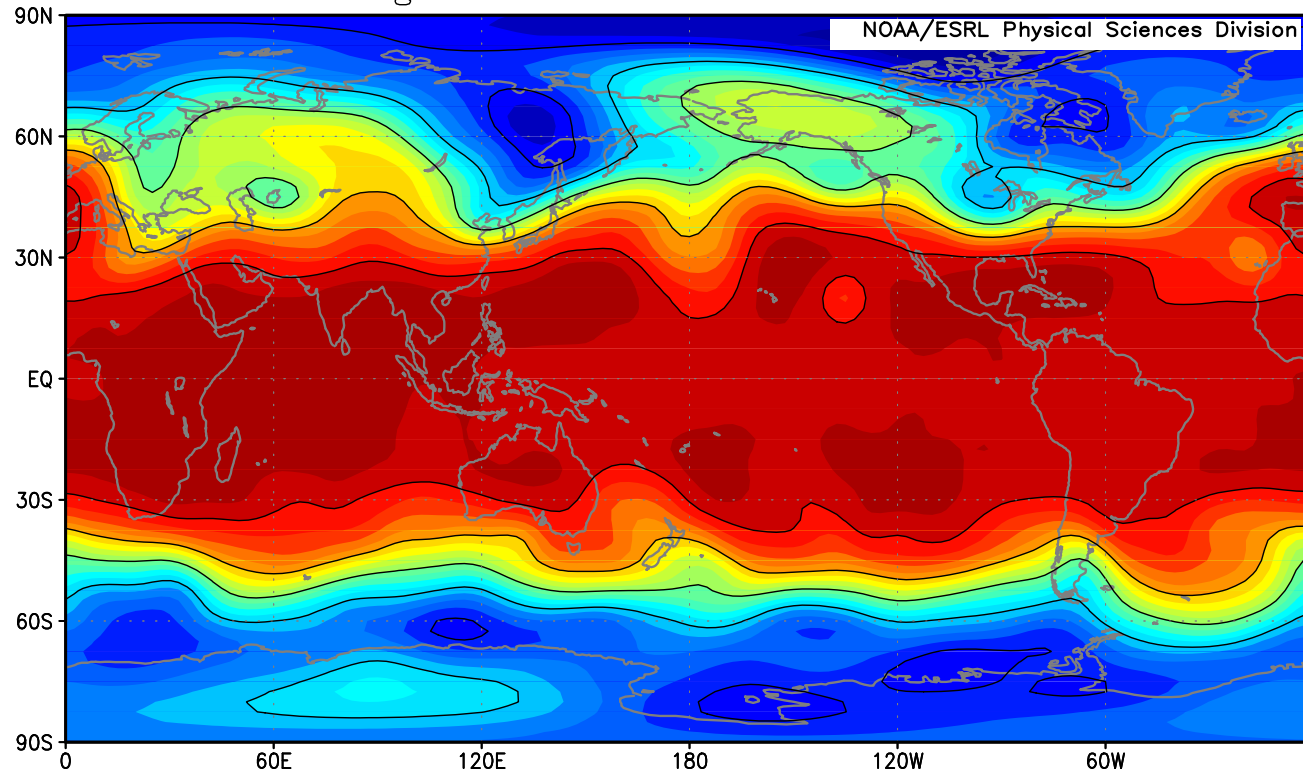


# Atmosphere: Mid-Troposphere Streamlines

December 21 2008 geopotential height

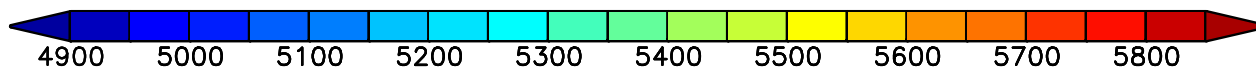
lon: plotted from 0.00 to 357.50  
lat: plotted from -90 to 90.00  
lev: 500.00  
t: Dec 21 2008 06 Z

Individual Obs hgt m



MAX=5892.6  
MIN=4860.74

GrADS image

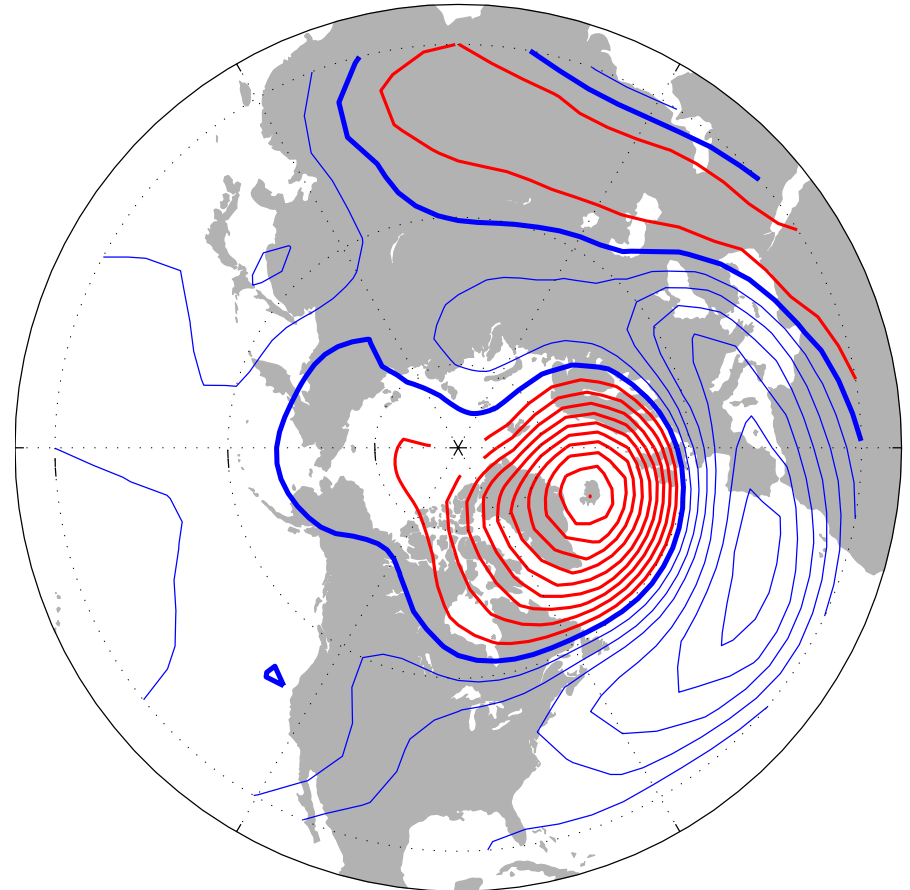
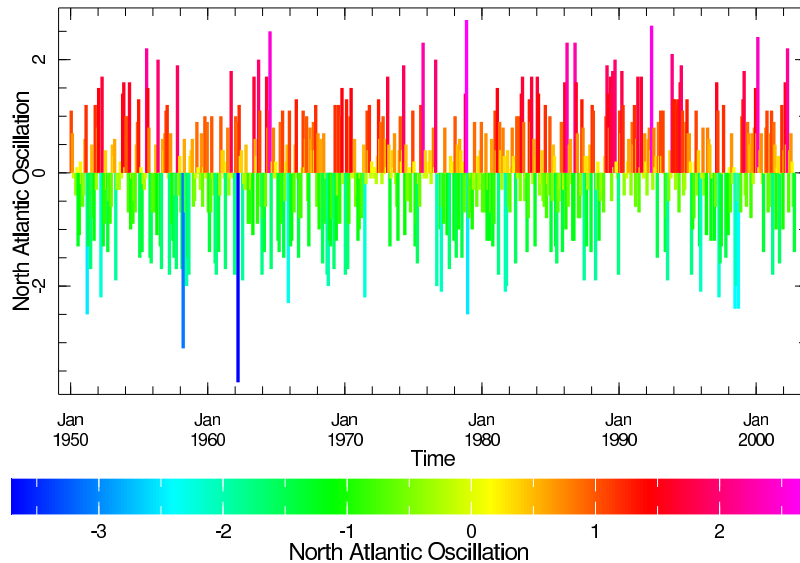


# Atmosphere: Large-Scale Teleconnections

**Teleconnections:** hemispheric-scale structures of atmospheric variability

## North Atlantic Oscillation (NAO)

One-Point Correlation Map

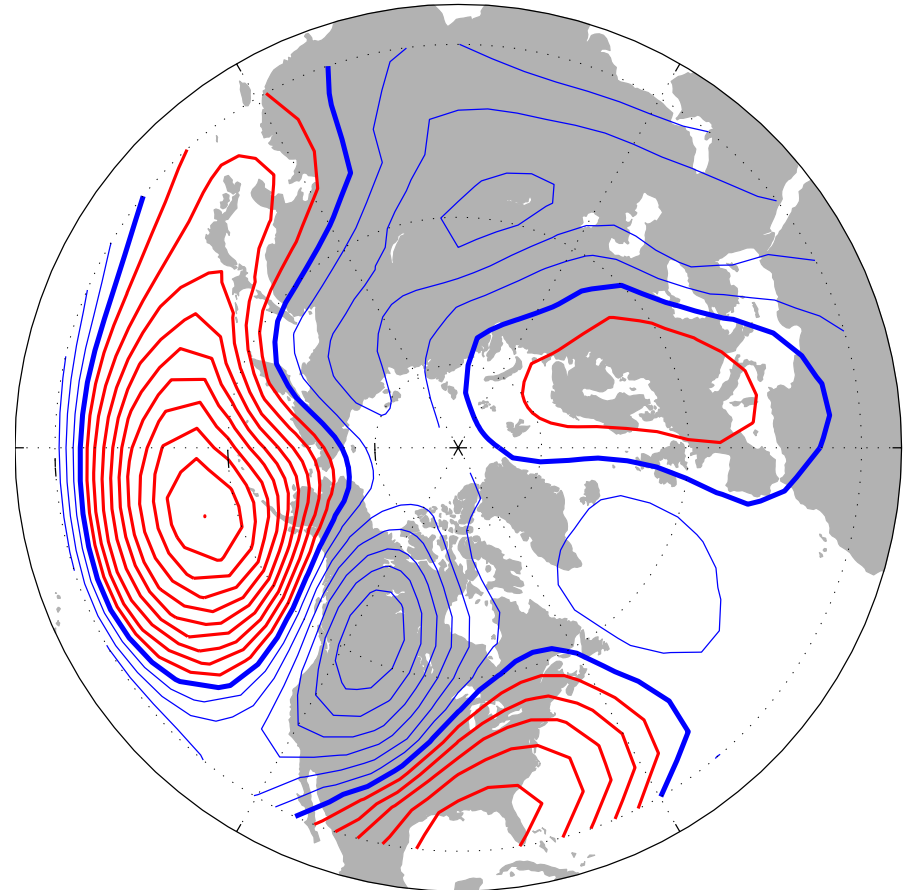
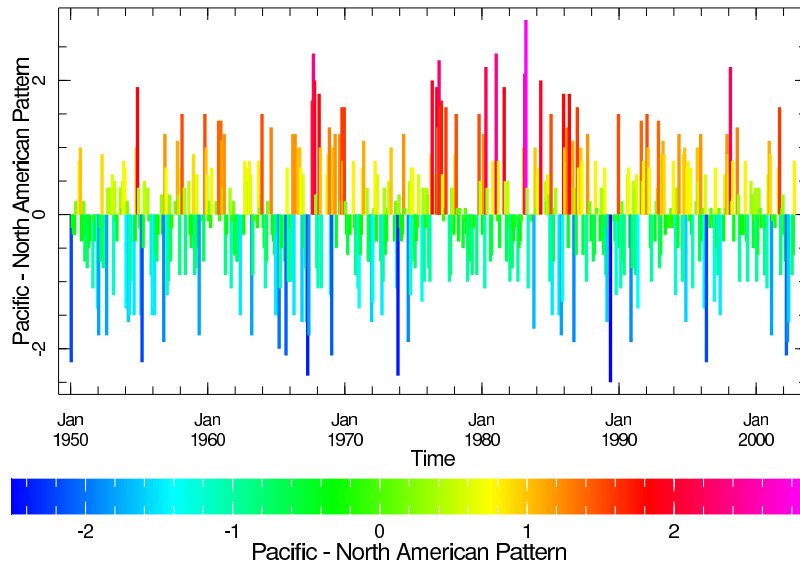


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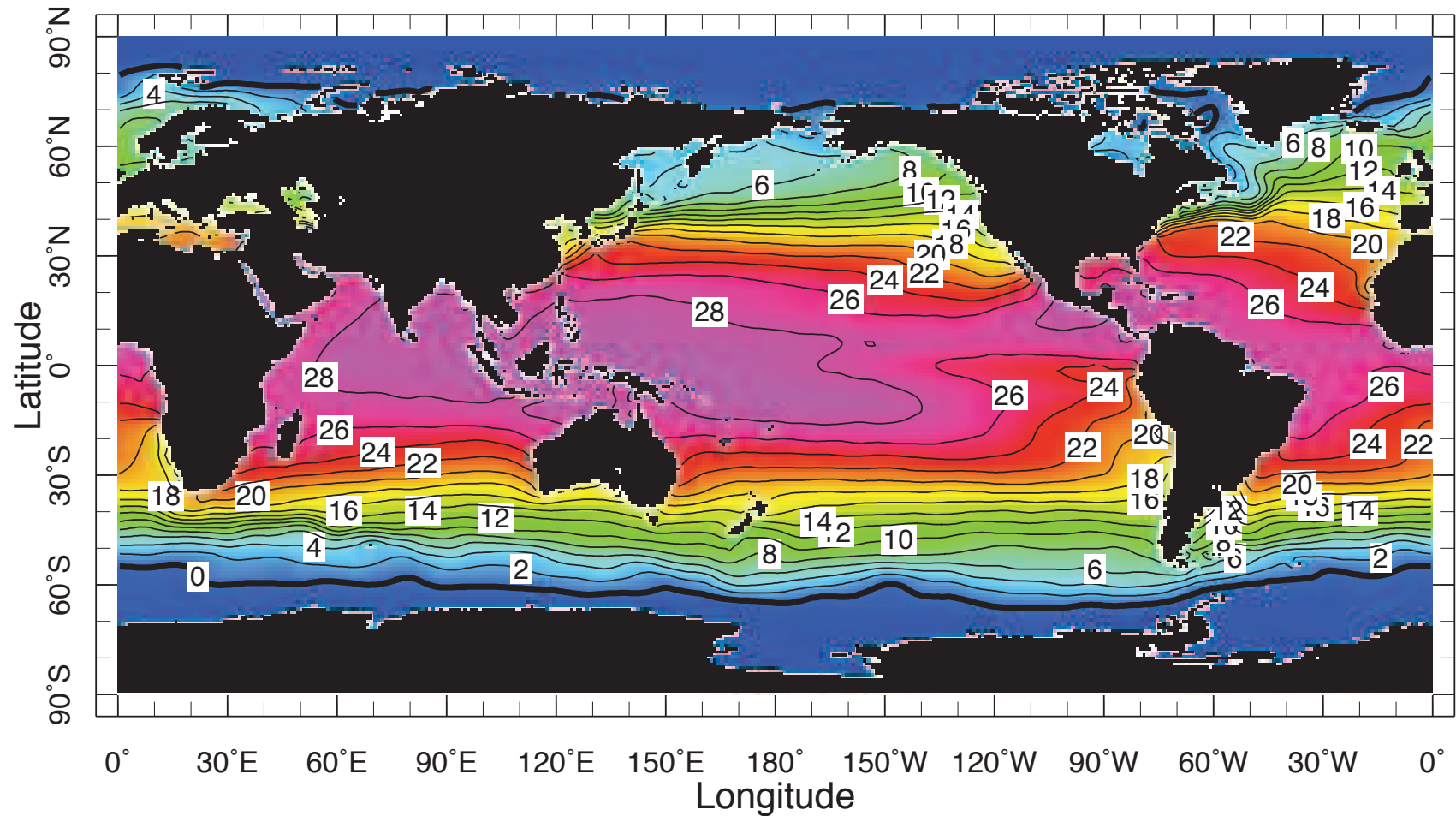
**Teleconnections:** hemispheric-scale structures of atmospheric variability

## Pacific-North America (PNA) Pattern

One-Point Correlation Map



# Ocean: Mean Sea Surface Temperature



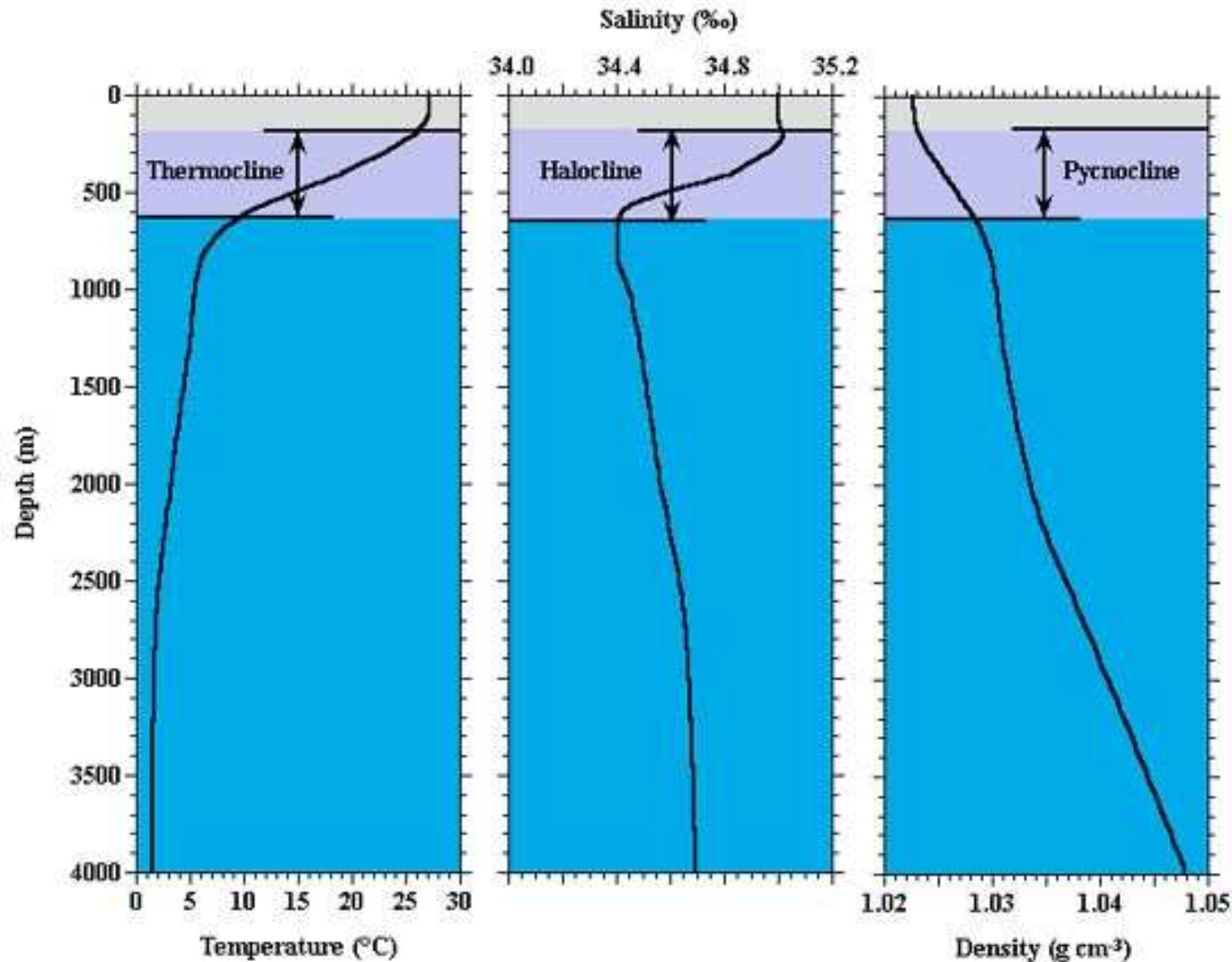
0.0 m

From World Ocean Atlas 2005 <http://ingrid.ldeo.columbia.edu>



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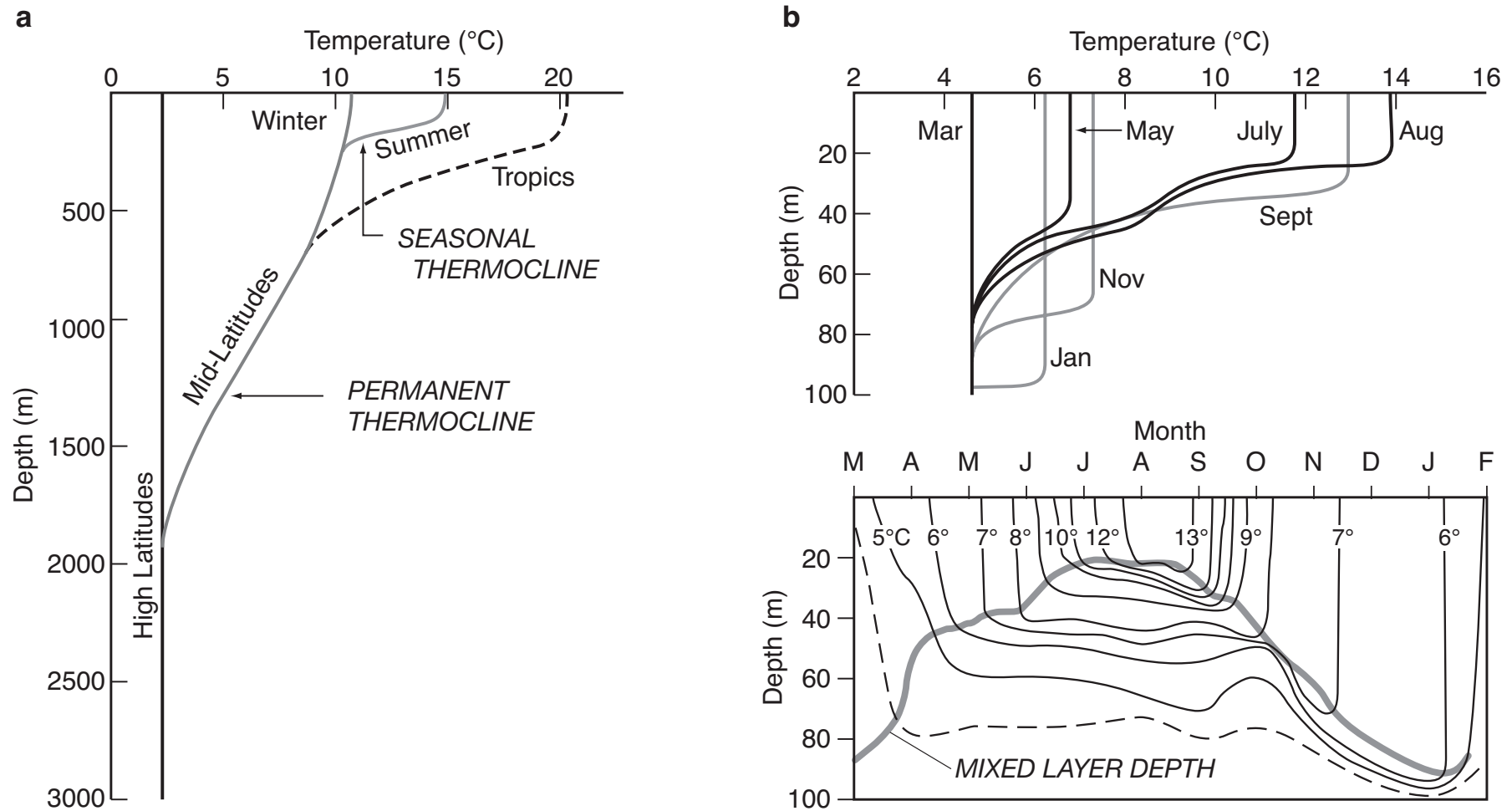
# Ocean: Typical Stratification



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From [http://ocp.ldeo.columbia.edu/climatekidscorner/ocean\\_stratification.jpg](http://ocp.ldeo.columbia.edu/climatekidscorner/ocean_stratification.jpg)

# Ocean: Mixed Layer Depth Variability



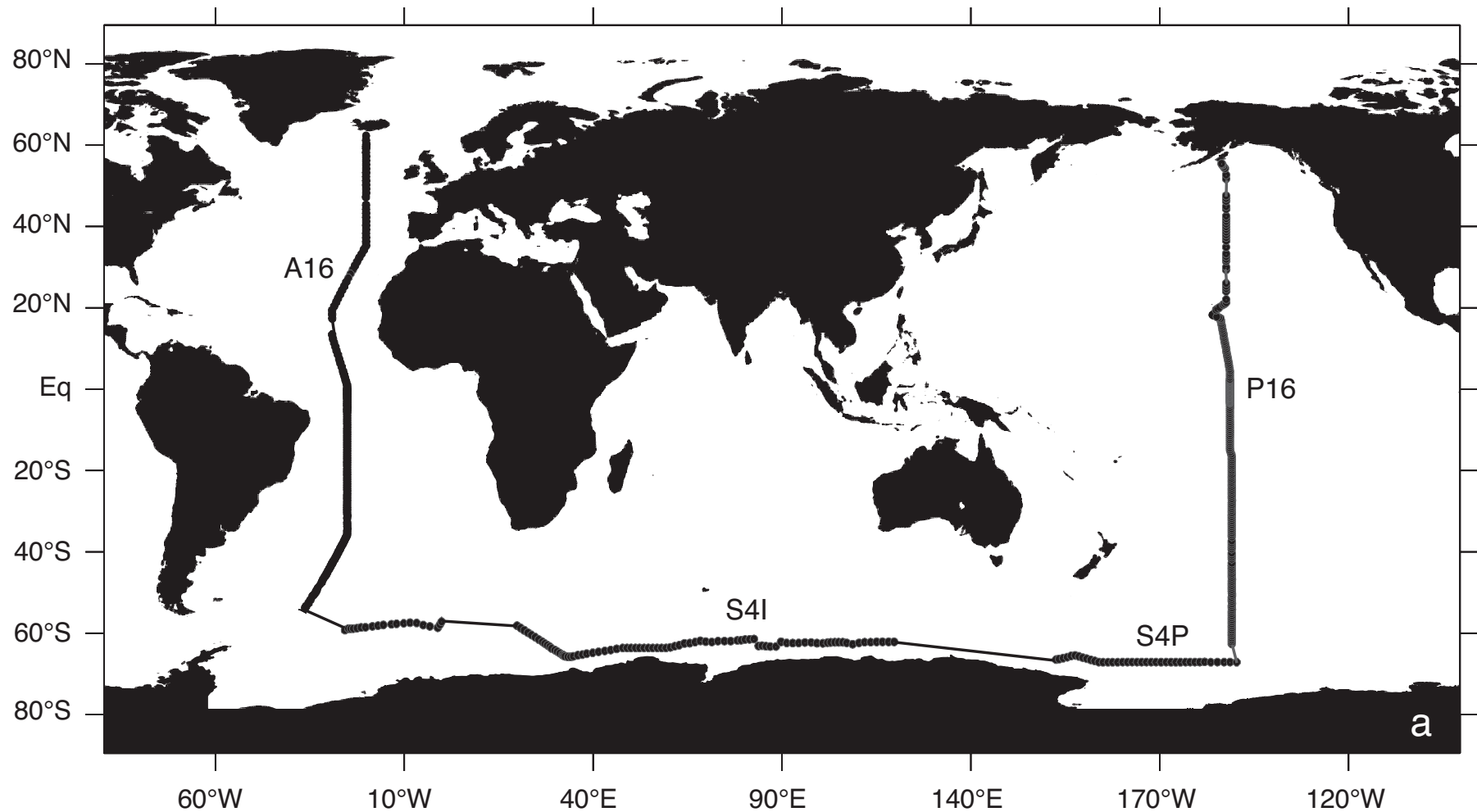
From Sarmiento & Gruber, Ocean Biogeochemical Dynamics, 2006



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# Ocean: Mean Thermal Structure

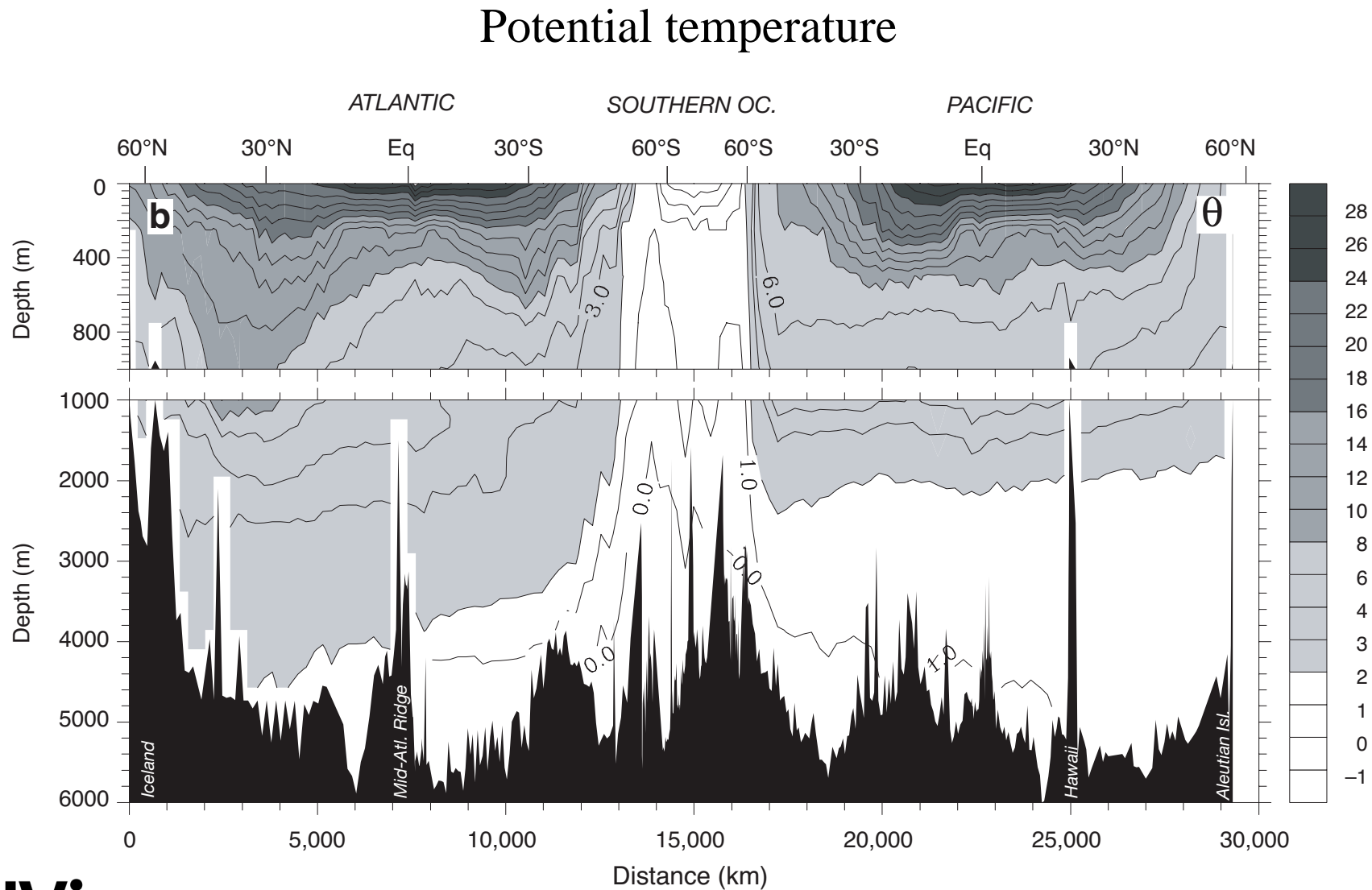
## Hydrographic sections



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From Sarmiento & Gruber, Ocean Biogeochemical Dynamics, 2006

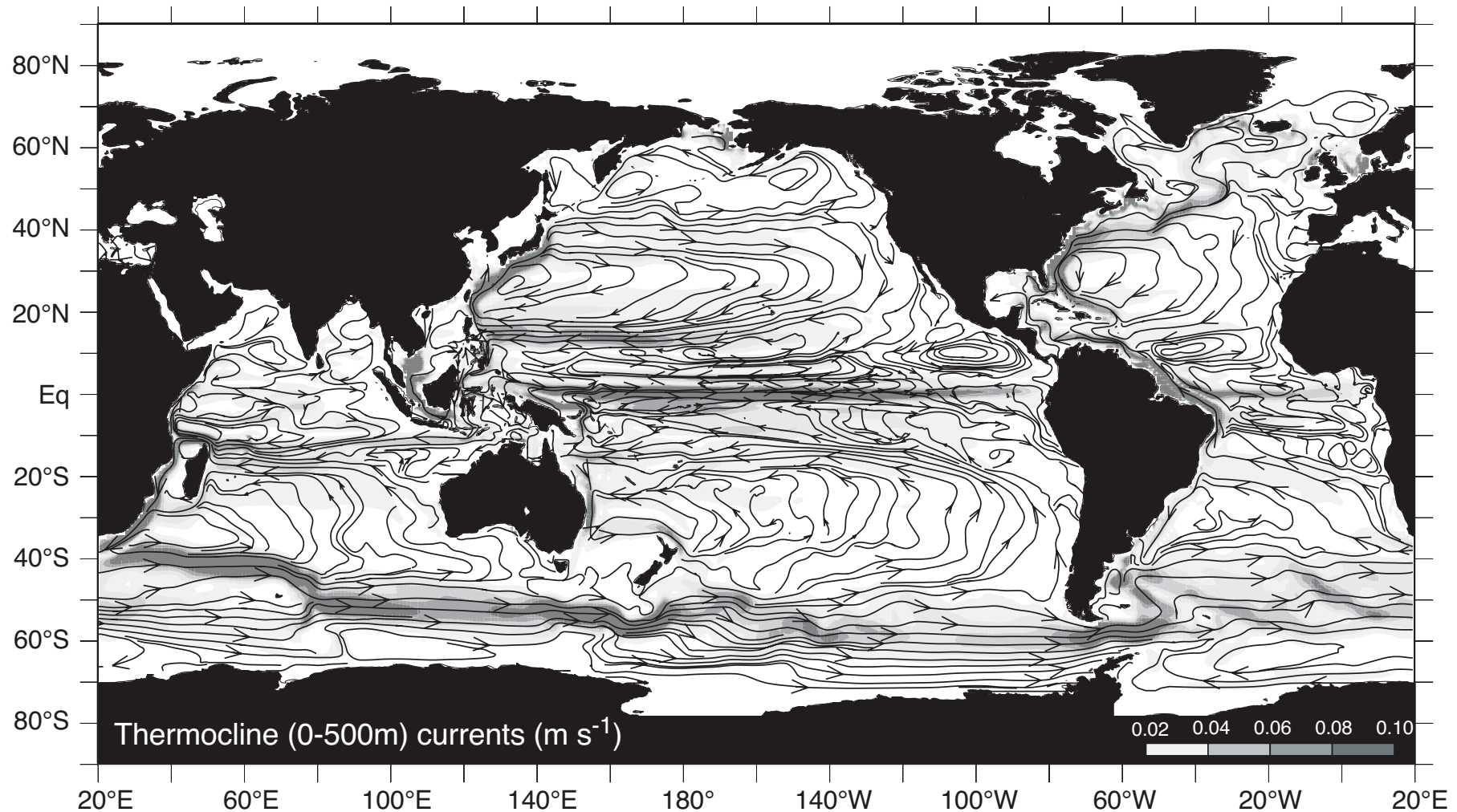
# Ocean: Mean Thermal Structure



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From Sarmiento & Gruber, Ocean Biogeochemical Dynamics, 2006

# Ocean: Mean Wind-Driven Currents



From Sarmiento & Gruber, Ocean Biogeochemical Dynamics, 2006

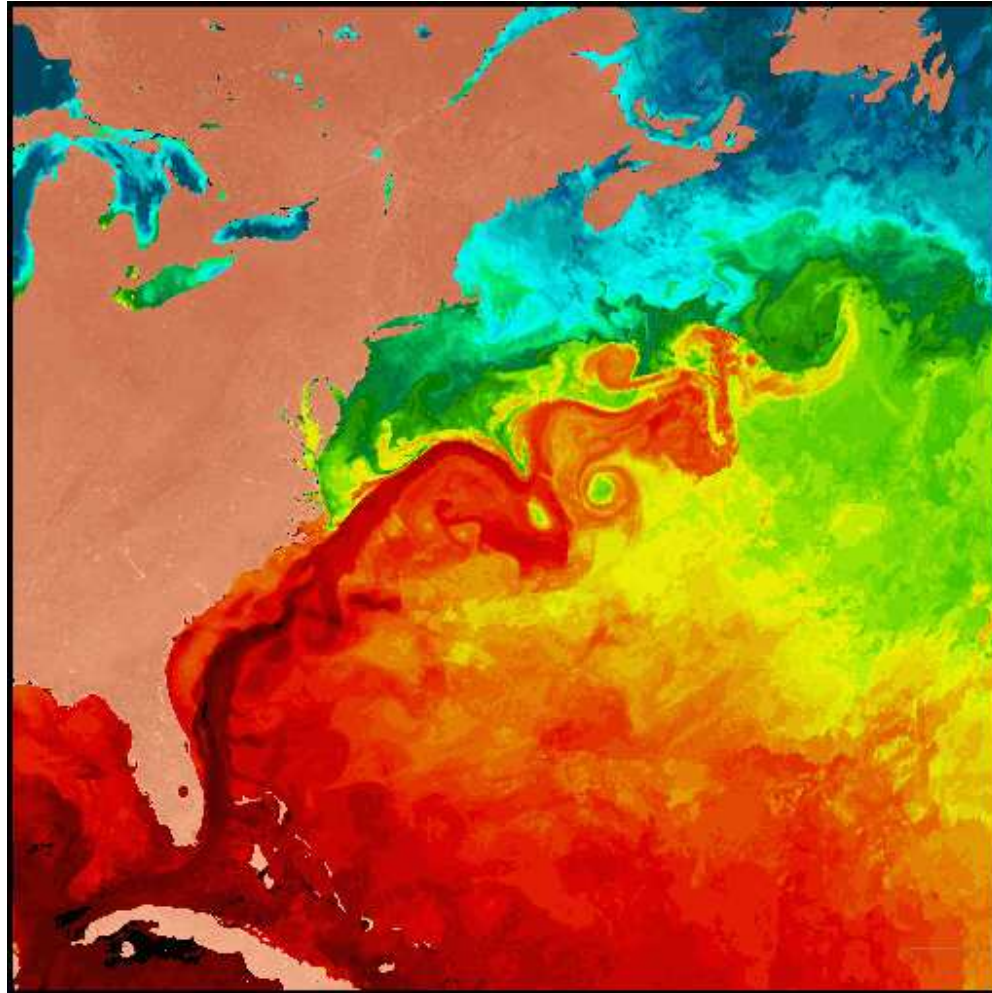


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# Ocean: Variability in Wind-Driven Currents

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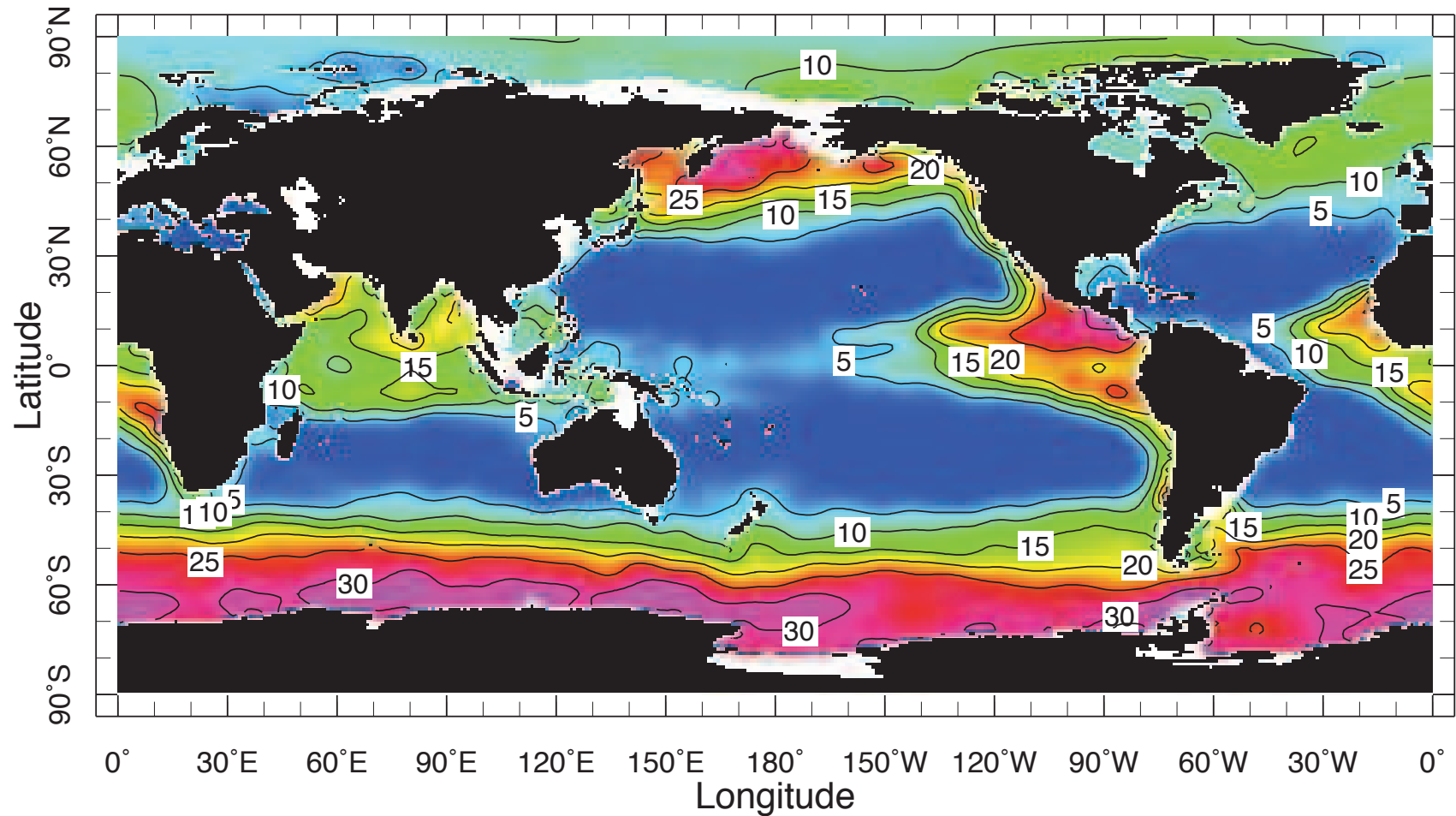
False colour SST image showing Gulf Stream eddies



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From <http://www.knmi.nl>

# Ocean: Mean 100m Nitrate Concentration



100. m

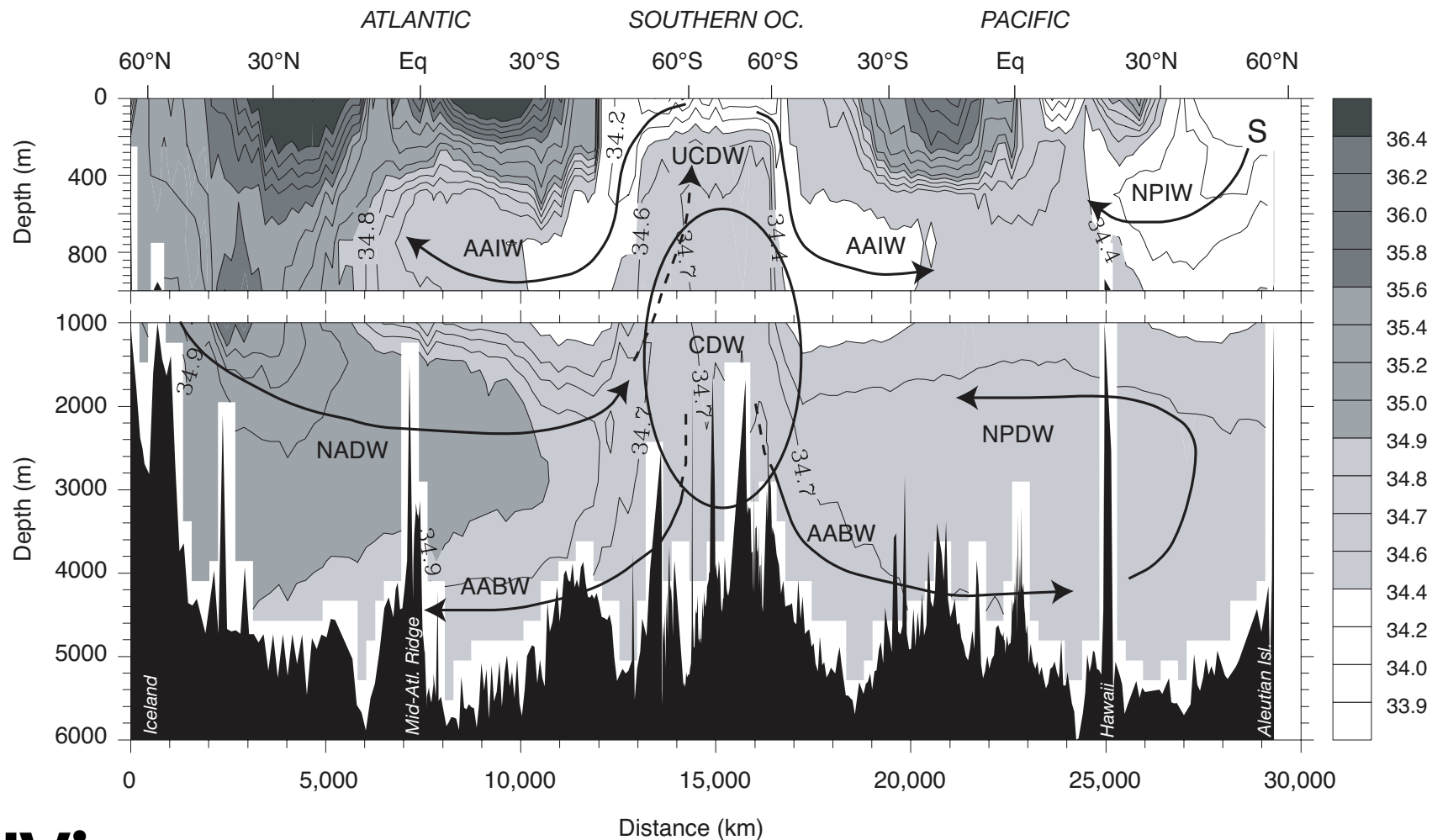
From World Ocean Atlas 2005 <http://ingrid.ldeo.columbia.edu>



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# Ocean: Deep Circulation

## Density distribution and water mass formation

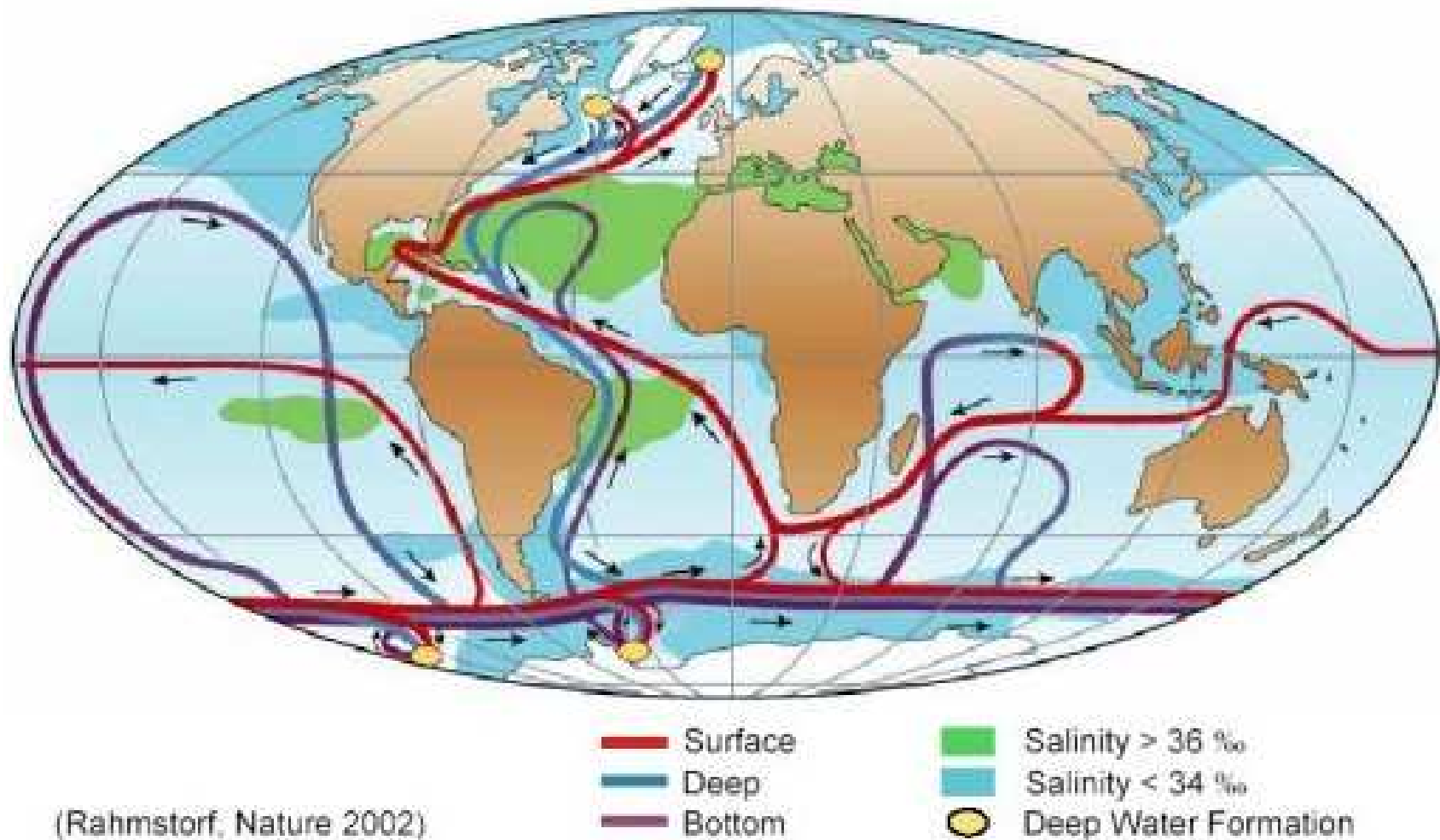


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From Sarmiento & Gruber, Ocean Biogeochemical Dynamics, 2006

# Ocean: Deep Circulation

Thermohaline circulation “conveyor belt”



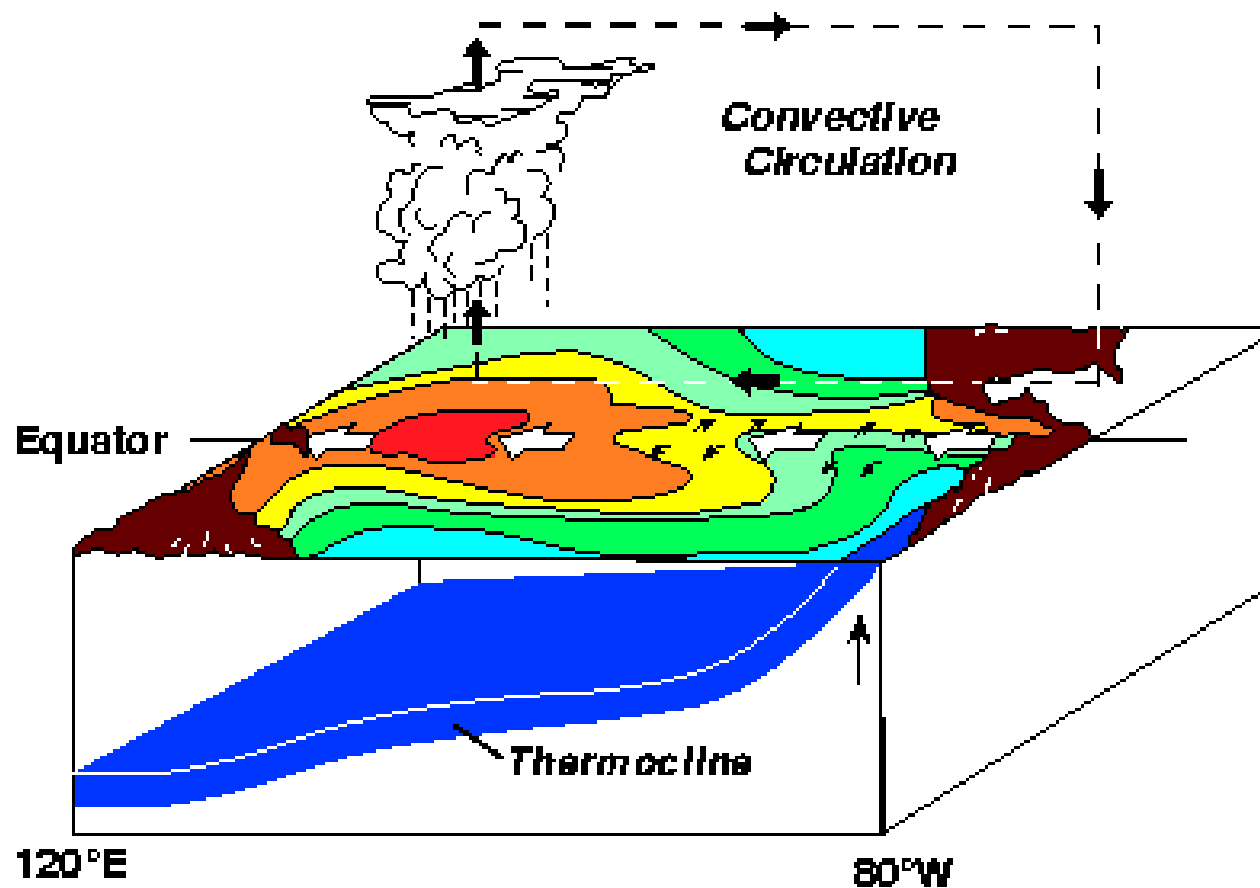
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From Kuhlbrodt et al., *Rev. Geophys.*, 2007

# Coupled Atmosphere-Ocean Processes: ENSO

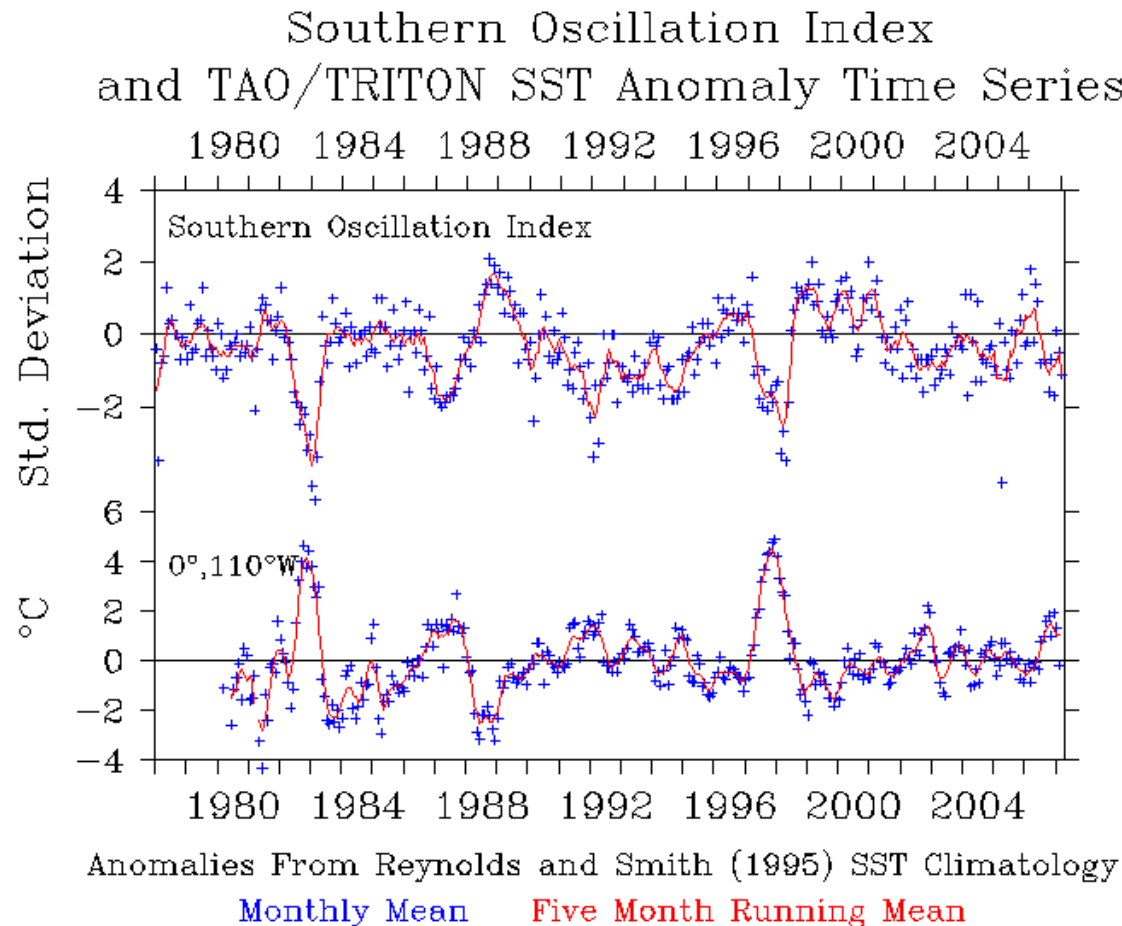
Mean State of Tropical Pacific

**Normal Conditions**



# Coupled Atmosphere-Ocean Processes: ENSO

## Tropical Pacific variability: Southern Oscillation Index & Nino 3.4 Index



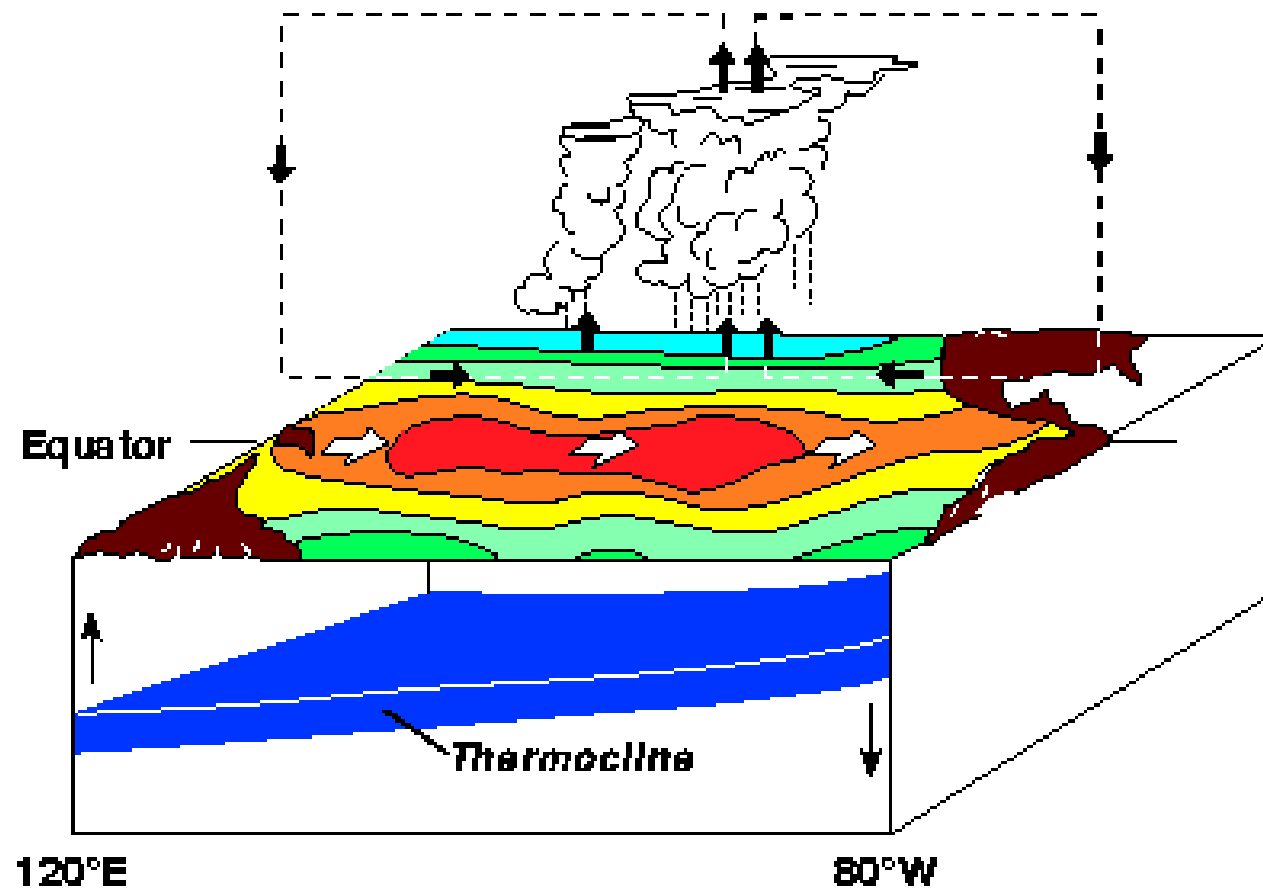
TAO Project Office/PMEL/NOAA

Mar 2 2007

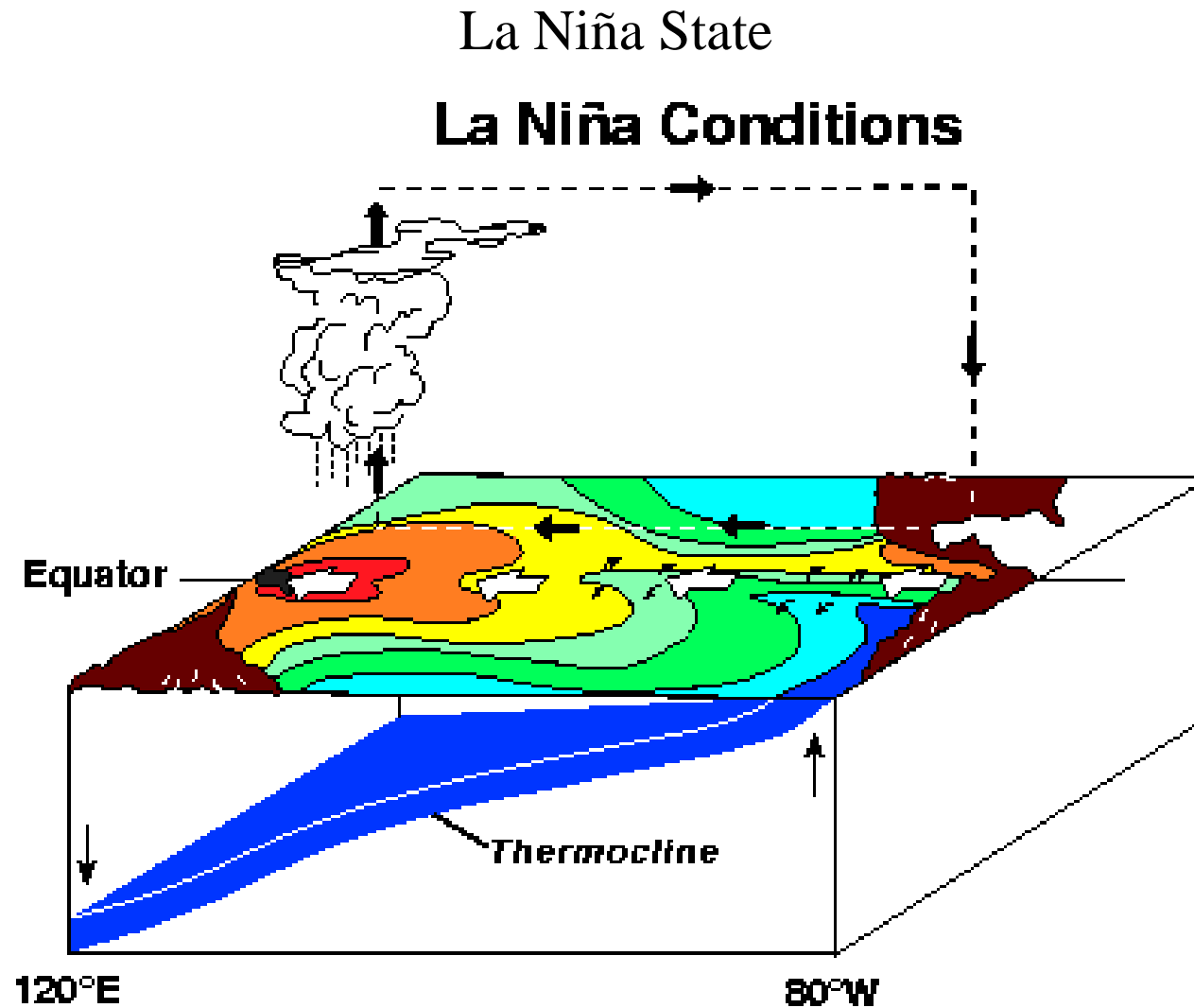
# Coupled Atmosphere-Ocean Processes: ENSO

El Niño State

**El Niño Conditions**



# Coupled Atmosphere-Ocean Processes: ENSO



From [http://www.pmel.noaa.gov/tao/el\\_nino/nino-home.html](http://www.pmel.noaa.gov/tao/el_nino/nino-home.html)

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    - hydrological cycle
  2. Ice

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    - land ice (ice sheets, glaciers, snow)

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  3. Biology, chemistry, etc ....

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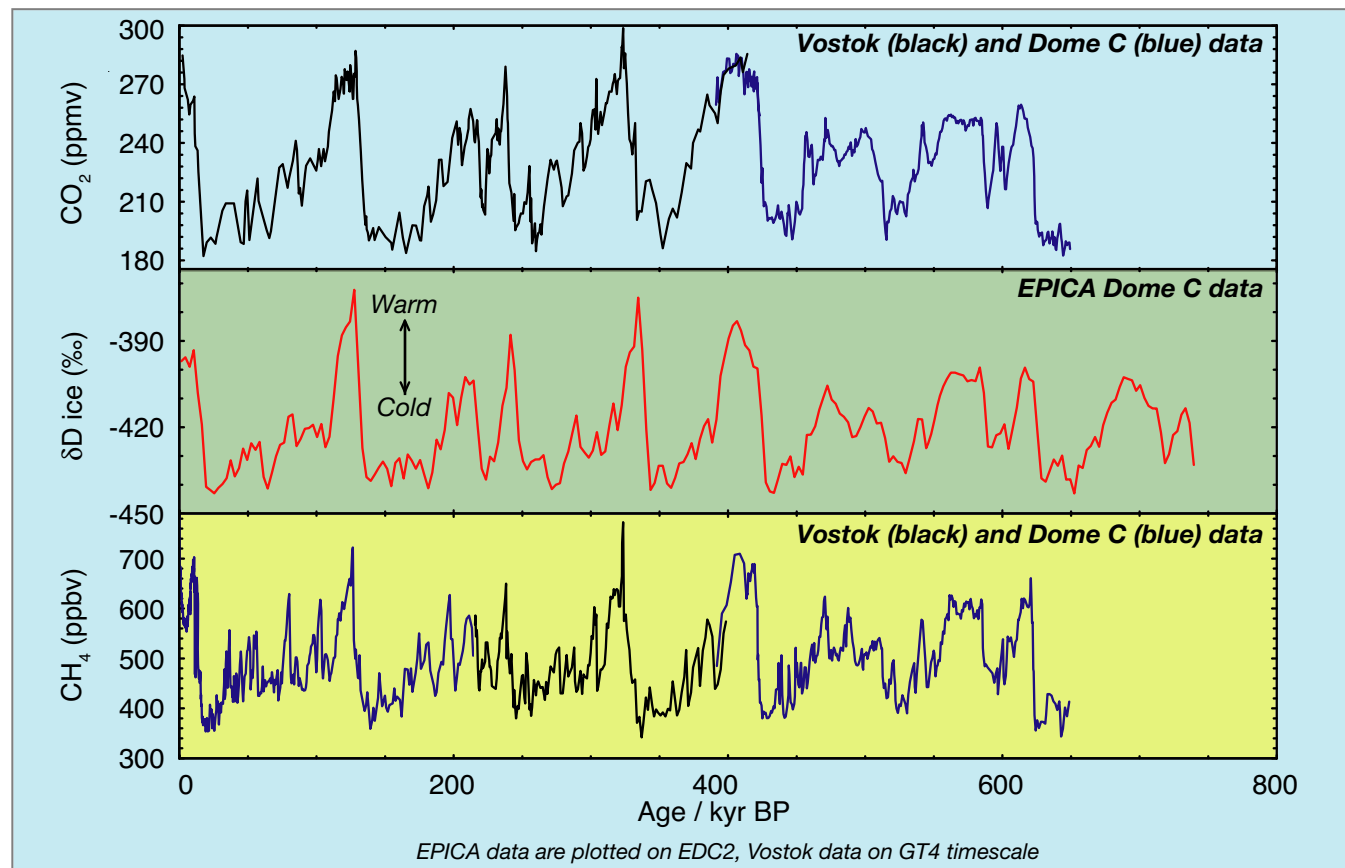
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    - sea ice
  3. Biology, chemistry, etc ....
    - Comprehensive studies of the system try to take all of these into account

# Climate Change

Ice core records: atmospheric composition and temperature

## Antarctic ice core records: Vostok and EPICA CO<sub>2</sub>, CH<sub>4</sub> and $\delta D$



GLOBAL  
I G B P  
CHANGE

Petit et al., 1999 (Vostok), Siegenthaler et al., 2005 (Dome C - CO<sub>2</sub>),  
Spahni et al., 2005 (Dome C - CH<sub>4</sub>), EPICA community members, 2004 ( $\delta D$ )

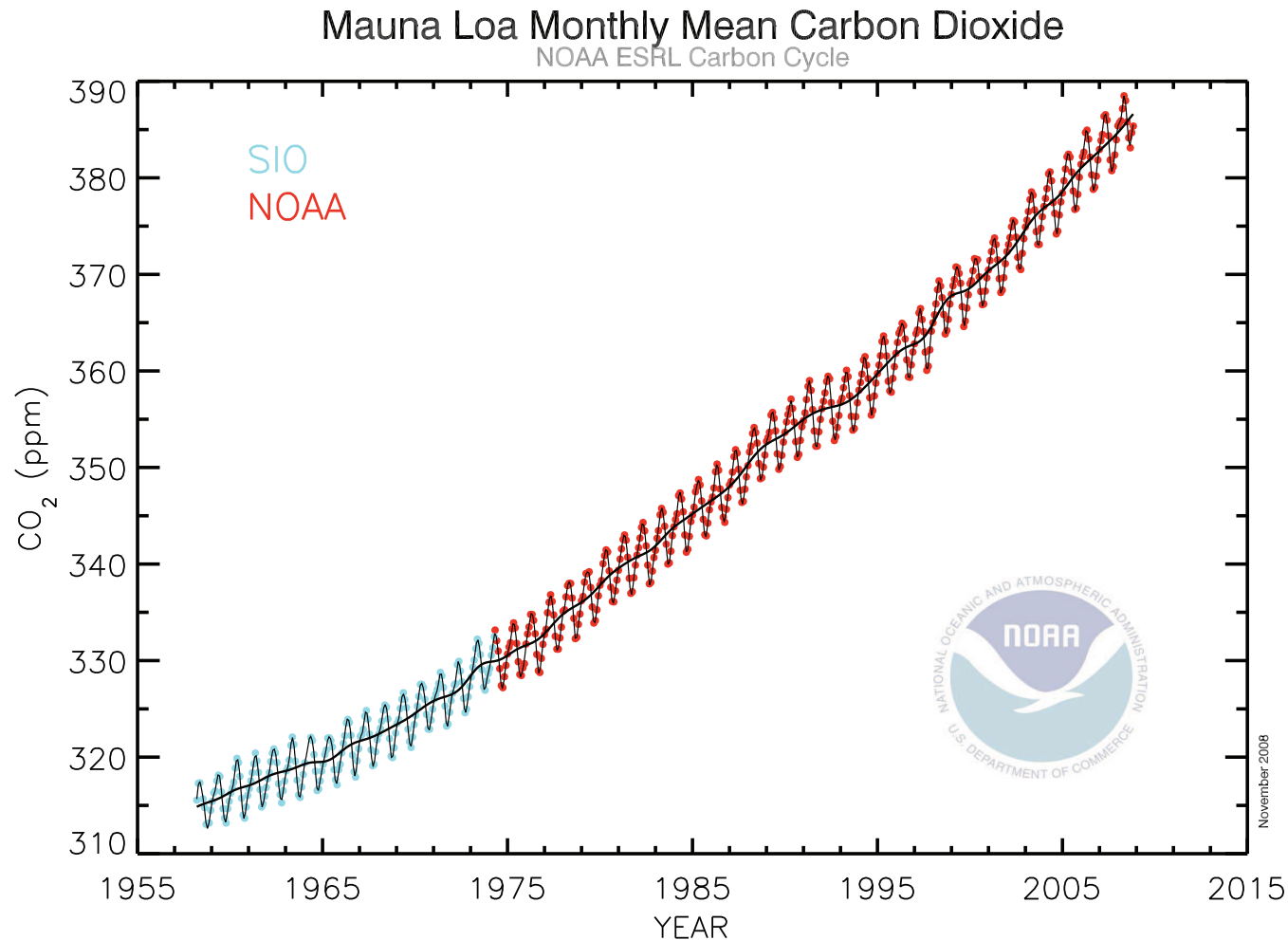
PAGES  
PAST GLOBAL CHANGES



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# Climate Change

## Mauna Loa CO<sub>2</sub> Record (the “Keeling Curve”)

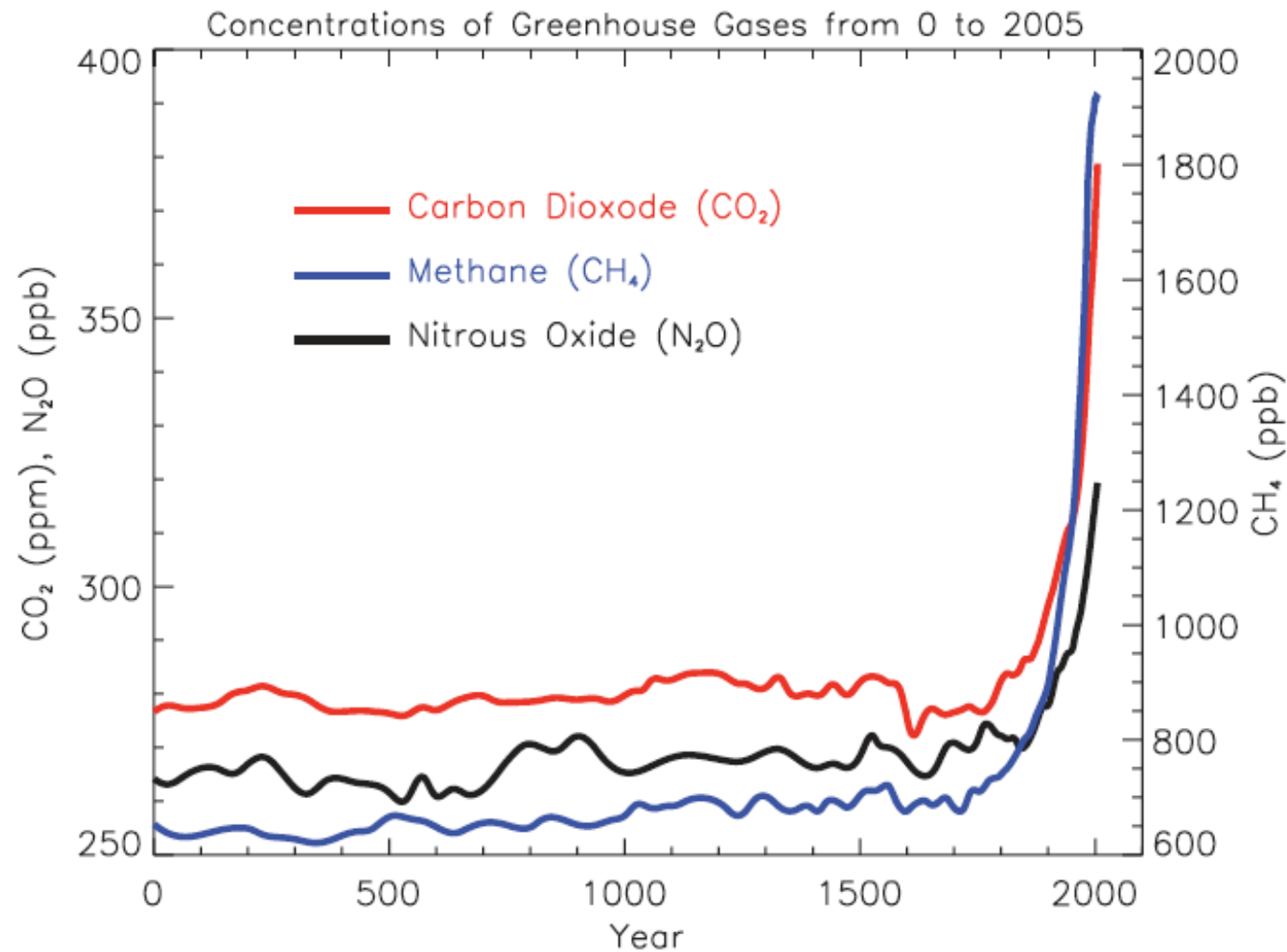


Atmospheric carbon dioxide monthly mean mixing ratios. Data prior to May 1974 are from the Scripps Institution of Oceanography (SIO, blue), data since May 1974 are from the National Oceanic and Atmospheric Administration (NOAA, red). A long-term trend curve is fitted to the monthly mean values. Contact: Dr. Pieter Tans, NOAA ESRL Carbon Cycle, Boulder, Colorado, (303) 497-6678, [pieter.tans@noaa.gov](mailto:pieter.tans@noaa.gov), and Dr. Ralph Keeling, SIO GRD, La Jolla, California, (858) 534-7582, [rkeeling@ucsd.edu](mailto:rkeeling@ucsd.edu).



UVic

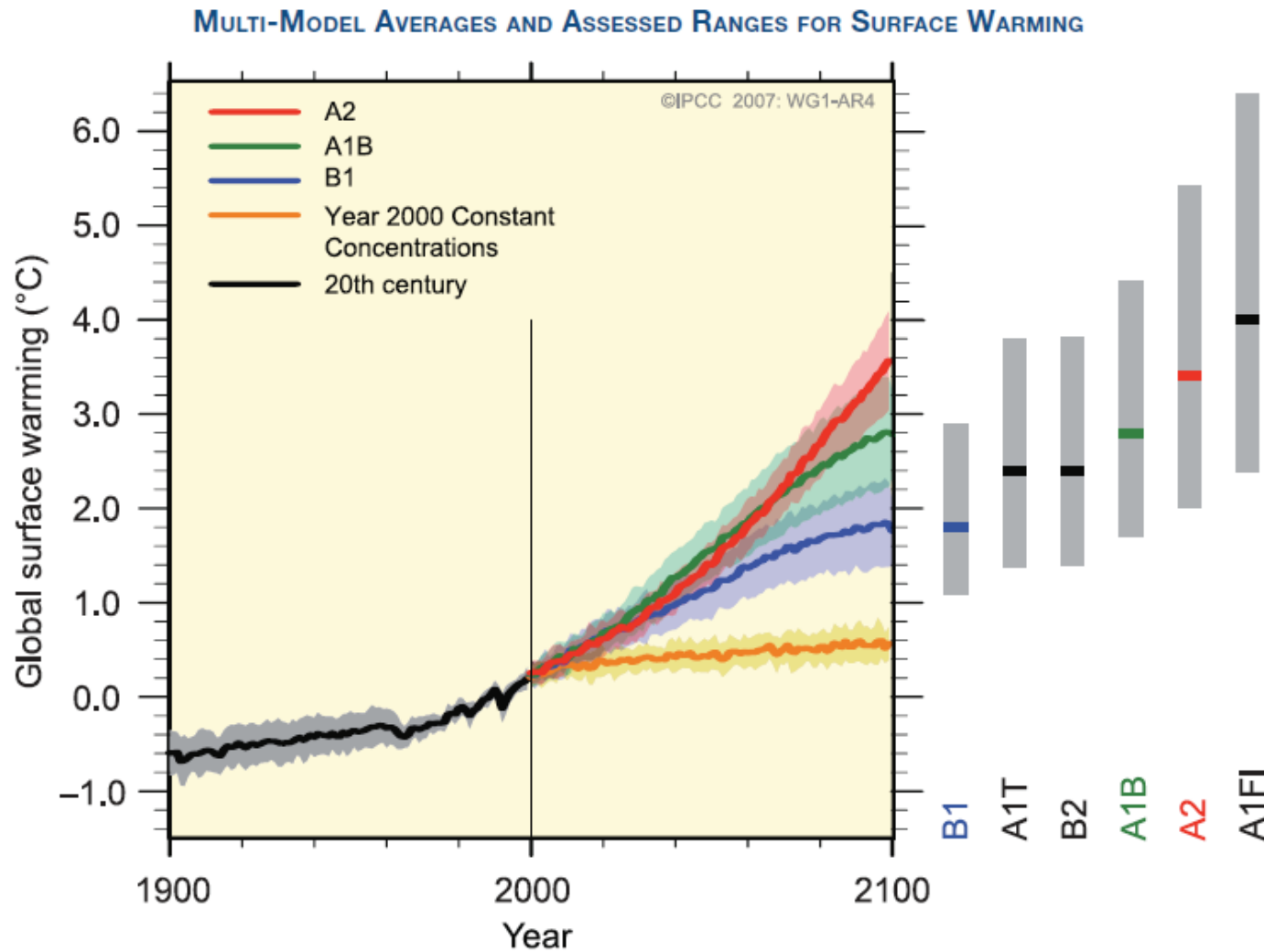
# Climate Change



UVic

From IPCC AR4 [www.ipcc.ch](http://www.ipcc.ch)

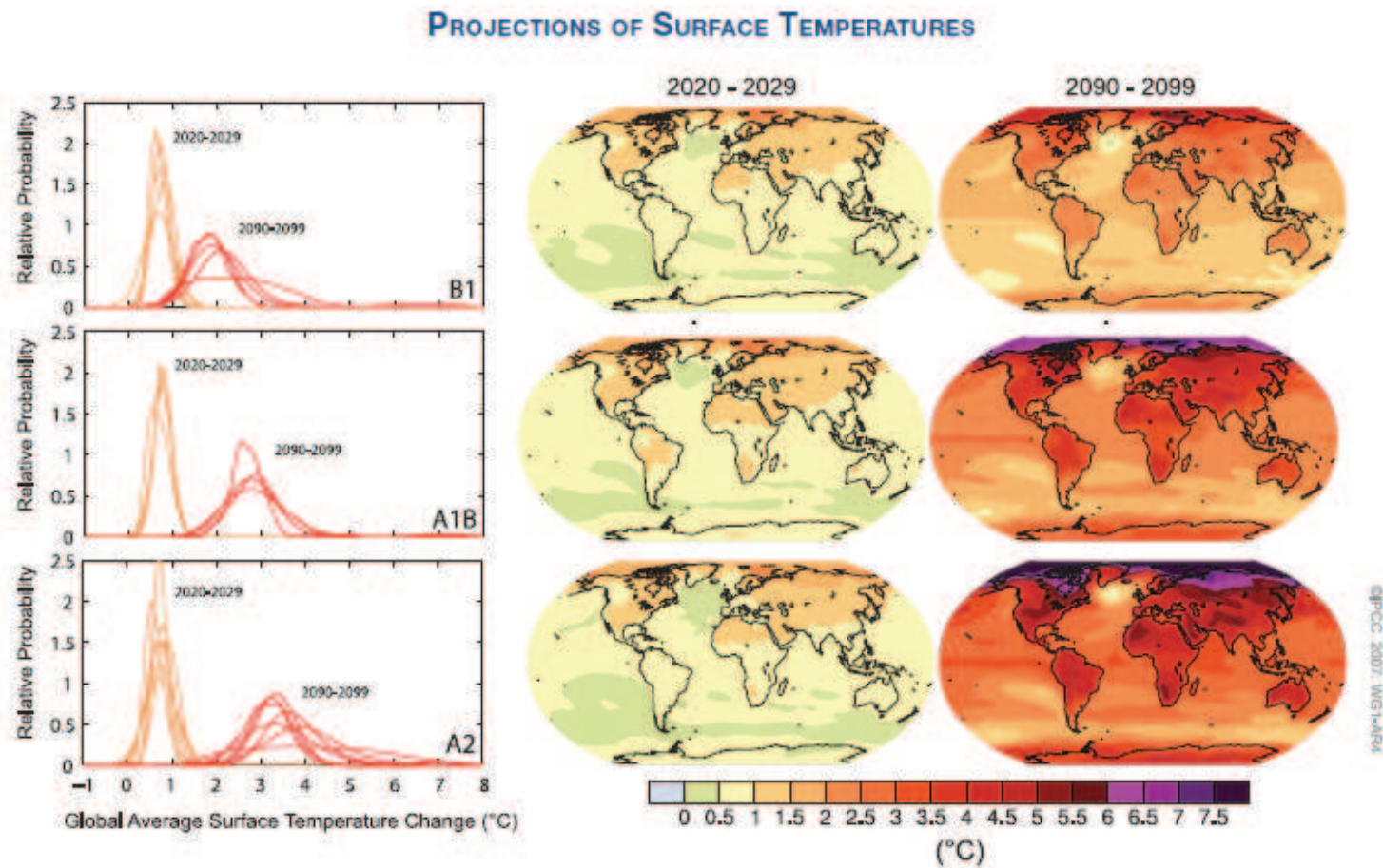
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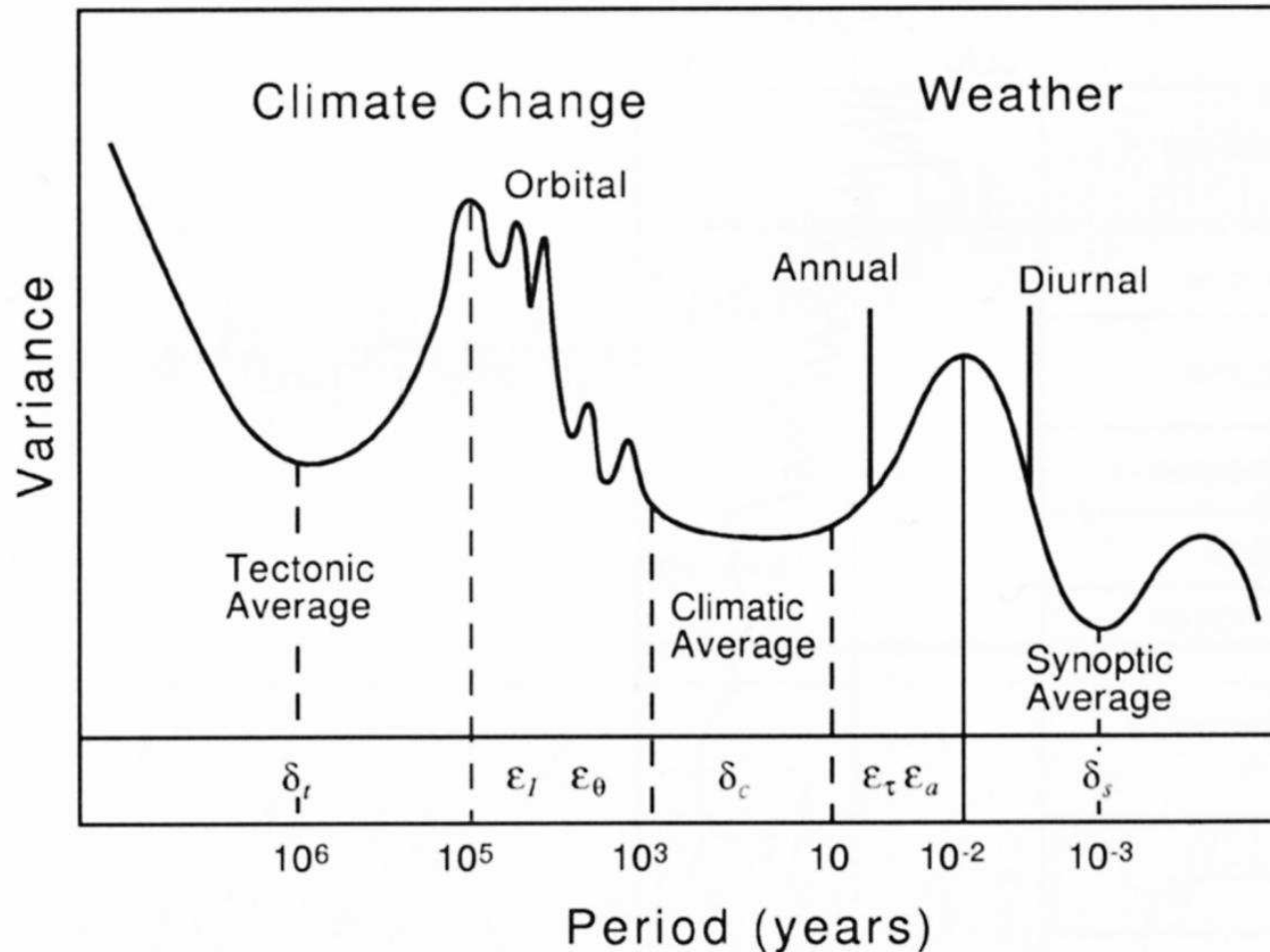
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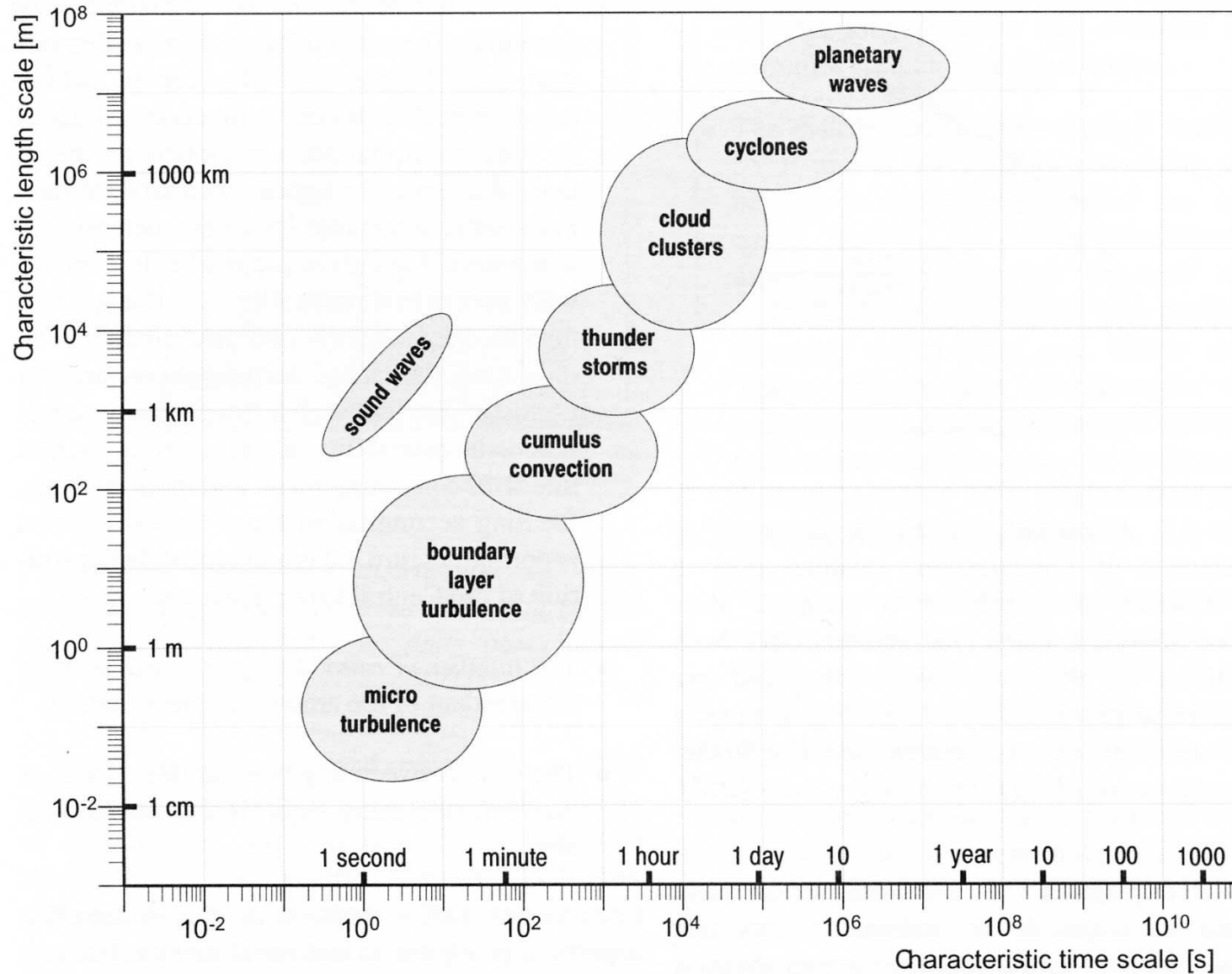
**UVic**

# Multiple Scales of Variability

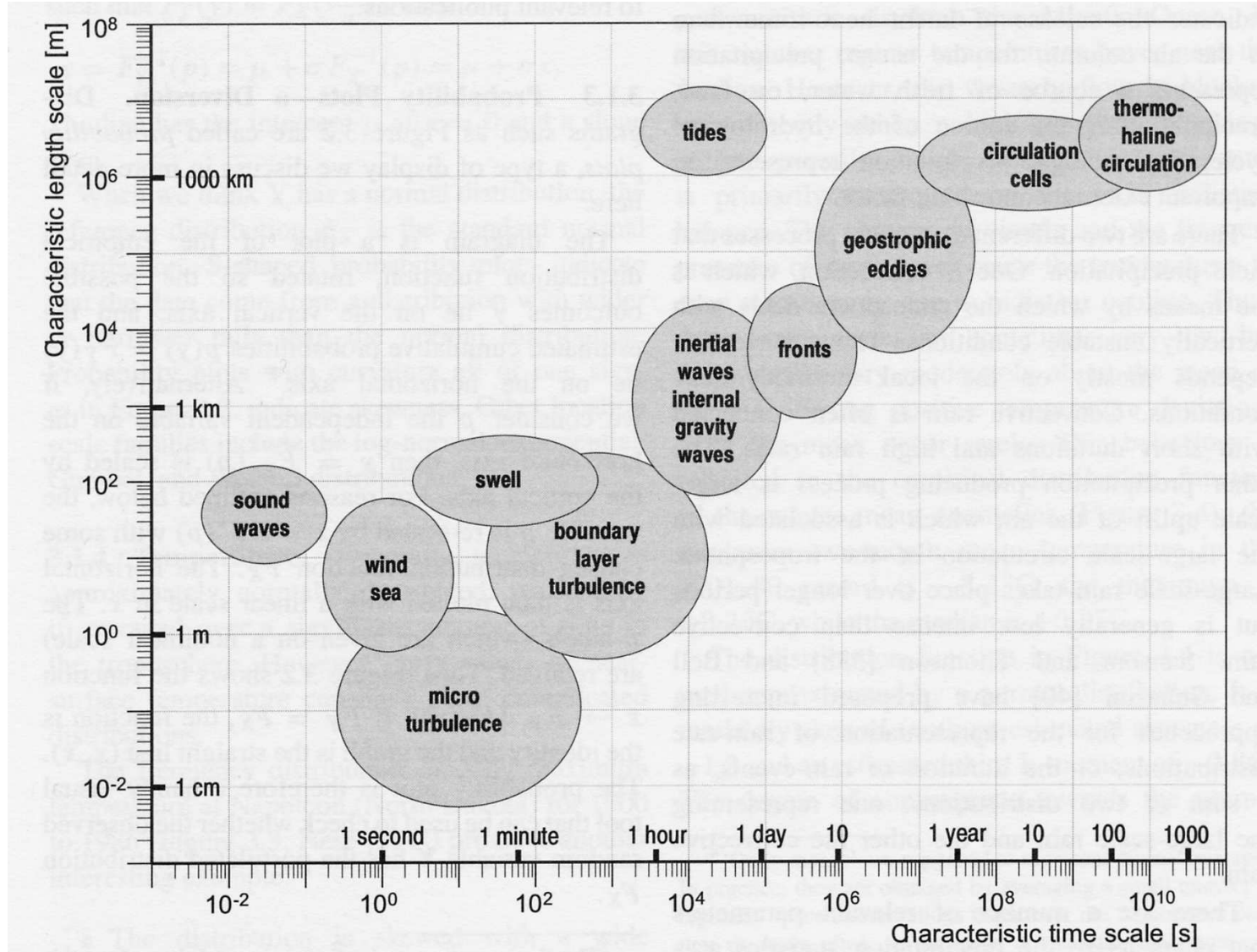
Climate system displays variability over broad range of space and time scales



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From von Storch and Zwiers, 1999



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# Probability and Climate

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[evolution of trajectory (“weather prediction”) **and** response of measure to forcing (“climate prediction”)]



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- A fundamental complication of the weather-climate connection is that **variability is coupled across scales**: fast weather influences the climate, and slow climate modulates the weather